

# Software Testing and Validation

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Corso di Laurea in Informatica

## Testing Methodologies

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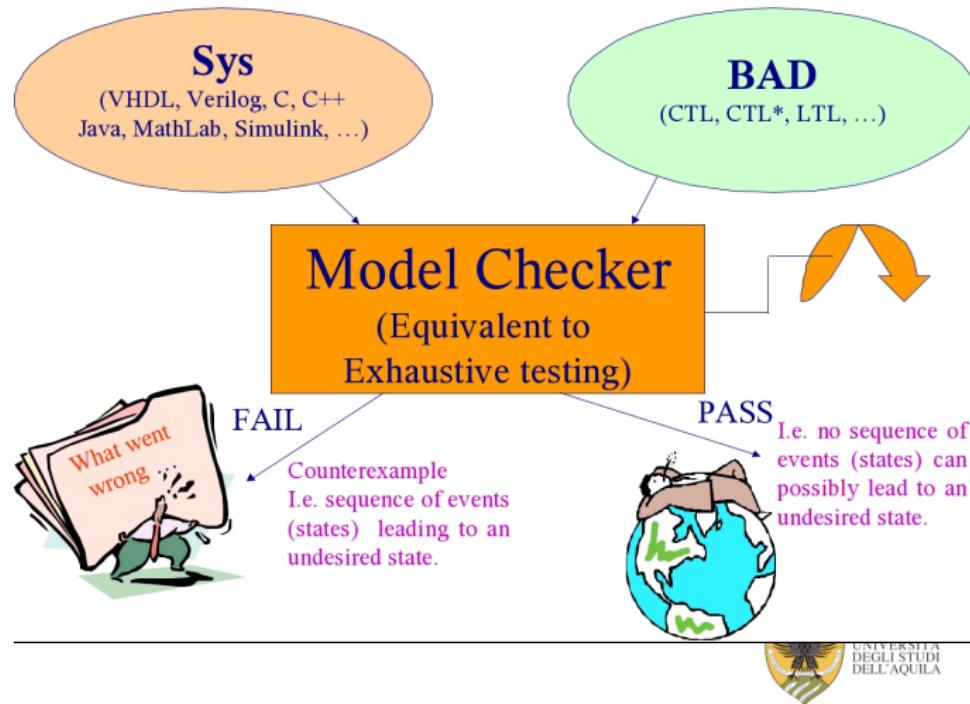
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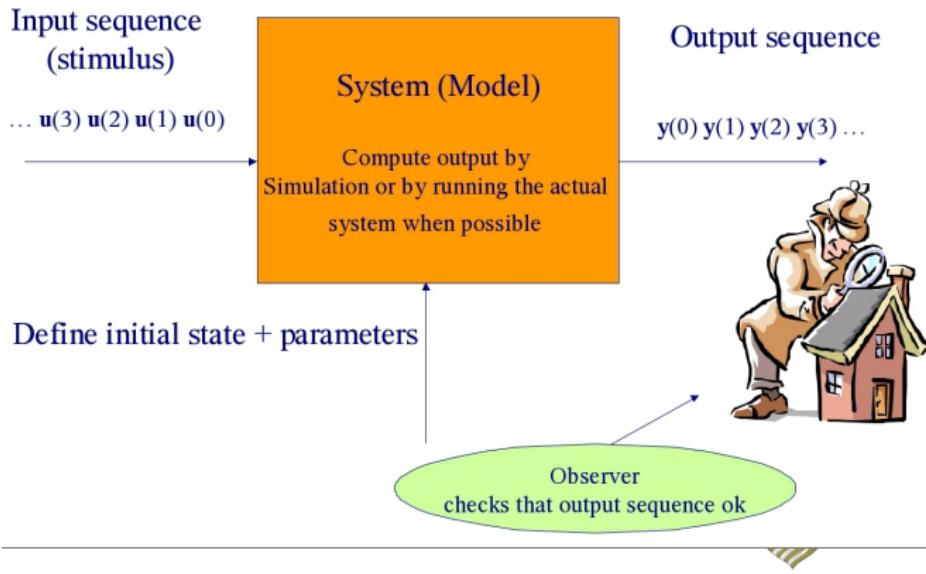


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# From Model Checking...



## An approximate answer BUG HUNTING: Testing + Simulation



# Testing AKA Get the Inputs

- Model Checking main difficulty:
  - choose the most suitable model checker
  - understand the system and model it within the model checker input language
  - understand the properties of the system and specify them within the model checker temporal logic
- Testing main difficulty: which inputs should I use?
  - slightly less difficult: how do I observe/check the result?
  - also running tests may be an issue
- Recall that inputs are theoretically infinite and practically too many
  - a function taking an input integer...
  - thus also important: which input coverage am I achieving?



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# Testing AKA Get the Inputs

- There are exceptions:
  - programs without inputs
    - e.g.: always returns the same constant, or a constant depending on previous executions
    - but one input is always present: launch the system...
  - programs taking enumerated inputs only
    - e.g.: a function taking two booleans
- In the vast majority of cases, too many inputs to consider them all, must somehow select a “meaningful” subset
  - i.e., so that errors, if present, are likely to be detected
- No general tools available, only some methodologies
  - good practices
  - some tools may be used for selected parts of the testing phase



# Terminology

## Program or System Under Verification (SUV)

- could also be a part of a “program”
- could also be a system with many processes

## Test case

A set of inputs, execution conditions, PASS/FAIL criterion

- input is anything the program to be tested can get
  - command-line arguments, files, interrupts, mouse coordinates, sensors...
- execution condition: information on the test execution
  - typically, input timing: whether all input must be provided at the start or not
  - e.g., a sequence of interrupts with given timing
- PASS/FAIL: some way to check
  - e.g.: output must be equal to this expected result



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# Terminology

**Test case specification** A formal or informal description of a test case

- “the input is two words” → a valid test case will be “goodbye all”

**Test suite** a set of test cases

**Test execution** running the test cases on the program

**Test obligation** a property for test case specifications

- e.g., “all words must be 7 letters long”

**Adequacy criteria** some property a test suite must fulfill

- e.g., “all test cases must contain at least 30 inputs”
- could also be seen as a set of test obligations
- namely, the adequacy criterion is satisfied if every test obligation is satisfied by at least one test case in the suite



# Terminology

**Function** Mathematical concept (set of pairs)

**Java Function** Syntactical function in Java language

- works with all other languages, of course

**Unit** Smallest unit of work in the program

- typically (but not always) close to single functions or single classes
- here, “unit of work” roughly refers to:
  - the smallest increment by which a software system grows or changes
  - the smallest unit that appears in a project schedule and budget
  - the smallest unit that may reasonably be associated with a suite of test cases (*unit testing*)



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# Terminology

**Independently Testable Feature (ITF)** Some functionality of the program which can be isolated from the other functionalities

- not necessary at code level: here, it is testing level
- e.g., a program or a function may be able to both sort and merge files
- however, sorting and merging may be ITF
- granularity depends on the program: from individual functions, to features of an integrated system composed of many programs
- going through individual classes and libraries
- when detected at unit testing, an ITF is usually a function/method or a class, but **not only unit** testing exists...



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# Testing Timeline

- 1 *Unit testing*
- 2 *Integration testing*
- 3 *System testing*
- 4 *Acceptance testing (validation)*
- 5 *Regression testing*



# Testing Main Techniques

- Two main overall methodologies:
  - *functional testing*: tester knows specs but not the code
    - also known as *black-box testing*
  - *structural testing*: tester exploits code knowledge
    - also known as *white-box testing* and *glass-box testing*
    - includes *data-flow testing*
- Applicable to all types of testing, from unit to acceptance
- Orthogonal and/or auxiliary techniques:
  - *combinatorial testing*
  - *model-based testing*



# Typical Setting for Testing

- Starting point: decide which is the SUV
  - not only up to the TE (Test Engineer)
  - must be also decided in accordance with developers and considering budget
- SUV may be:
  - a simple stand-alone program (unit + acceptance testing)
  - a system composed by a few interacting components (unit + integration + acceptance testing)
  - a prototype of a complex system with many interacting components (unit + integration + acceptance testing)
  - a complex system tout court (all testing)
    - for cyber-physical systems, this might include simulators
    - regression testing for something already tested
- A SUV always includes at least one ITF
- Acceptance and regression testing will be covered later, as they require special methodologies



# Typical Setting for Testing

- ① Given a SUV, the TE must develop:
  - a set of test case specifications (test suite)
  - test adequacy for the overall test suite
- ② TE generates the test cases from the test case specifications
- ③ TE runs the test and collect the results
  - test are instrumented so as to also check adequacy criteria
- ④ If adequacy criteria are not met, revise test case specifications going back to step 1
- ⑤ Developers correct all discovered errors and TE starts again from 3
  - no need to wait for the step 4: as soon as an error is discovered, it can be corrected
  - it may happen that specifications should be updated too → back to step 1



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## Example (White-Box Testing)

```
public static String collapseSpaces(String argStr)
{
    char last = argStr.charAt(0);
    StringBuffer argBuf = new StringBuffer();

    for (int cldx = 0 ; cldx < argStr.length(); cldx++)
    {
        char ch = argStr.charAt(cldx);
        if (ch != ' ' || last != ' ')
        {
            argBuf.append(ch);
            last = ch;
        }
    }

    return argBuf.toString();
}
```



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# Example (Black-Box Testing)

We have a function taking one string  $s$  as an input and returning a string  $s'$  as an output.

Informally:  $s'$  is the same as  $s$ , but *consecutive* spaces are collapsed into one space.

Formally: let  $S = \{(i, k) \mid s_i = ' ' \wedge (i > 1 \rightarrow s_{i-1} \neq ' ') \wedge k > 1 \wedge \wedge_{n=1}^{k-1} s_{i+n} = ' '\}$ . Let

$S' = \{(j, k) \mid \exists (i, k) \in S \wedge j = i - \sum_{(i', k) \in S \mid i < i'} (k - 1)\}$ . Let  $\sigma(S, j) = \sum_{(i, k) \in S \mid i < j} (k - 1)$ .

Then, for all  $j = 1, \dots, |s| - \sum_{(i, k) \in S} (k - 1)$ ,  $s'_j = s_{j + \sigma(S', j)}$



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# Example

- Test case specification 1: all input should be at least 10 characters long
- Test case specification 2: all input should contain at least 3 spaces
- Test obligation 1 (black-box): the test suite should contain an empty string
- Test obligation 2 (white-box): in the `if`, the first clause should always evaluate to true and the second to false at least once (and/or viceversa)
- We generate the test suite following specifications
- We check if obligations are ok



# Example

- Test obligation (*coverage*): all statements should be executed at least once
- What happens if the code has some unreachable code? No test suite is adequate!
- Quantitative measures could be used
- Suppose an adequacy criterion generates  $n$  obligations...
- ... if  $m$  of such obligations are met by the test suite, then it is  $100 \frac{m}{n} \%$  adequate



# Functional Testing

- Typically, we do not only have a program: we also have a functional specification of its behaviour
  - in some logic, or even in natural language (starting comments of a function...)
  - requirements are expressed by users and specified by software engineers
- Functional specifications are the base for functional testing
- More precisely, *functional test case design* is about deriving test cases from functional specifications
- The structure of the program is completely ignored
  - e.g., “all ifs must be evaluated at least once” is not functional testing
- Also called *black-box* testing
- Cheaper than white-box or glass-box testing

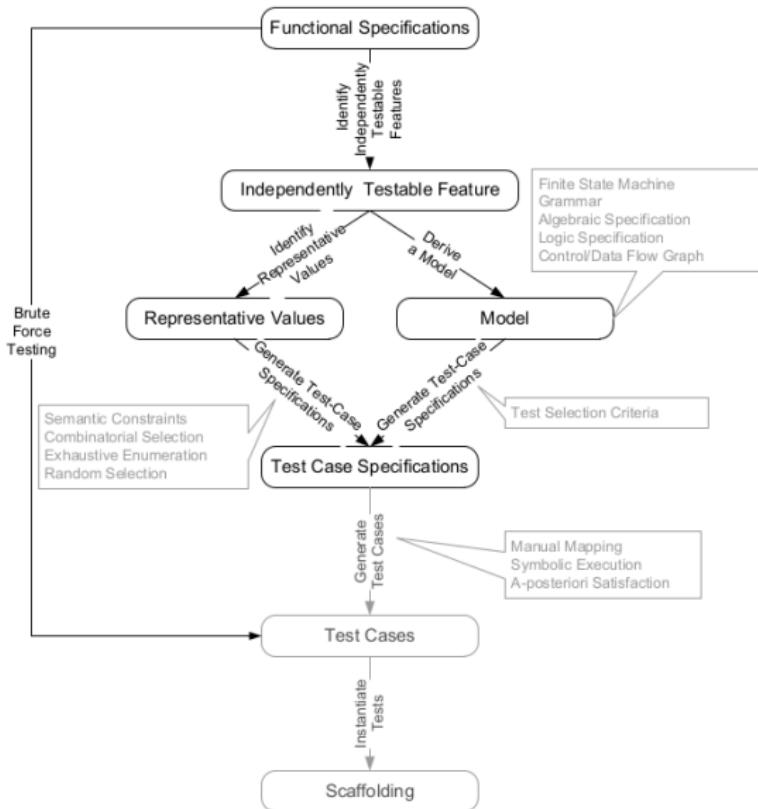


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# A Systematic Approach for Functional Testing



# A Systematic Approach for Functional Testing

- Step 1 is to identify “separated” features
  - lack of documentation may make this difficult
- Identify Independently Testable Features in unit testing
  - if it is a single function/method, probably just one ITF is possible
  - though there are functions where some parameters may trigger completely different behaviours
    - e.g., a Python function taking a list and a further argument telling what to do (average, summation, standard deviation, ...)
  - if it is a class, many ITFs are identifiable
    - e.g., for a String class, one ITF may be string creation and modification, another ITF may be string searching, ...



# A Systematic Approach for Functional Testing

- Identify Independently Testable Features in integration testing
  - for an FTP software, given the two units which directly exchange through a socket, an ITF may be the correct sending and receiving of any stream of bits
- Identify Independently Testable Features in system testing
  - web page specification: search the DB, update the DB, provide info from the DB
  - sub-functionalities: edit a pattern to search the DB, provide a form for registering, ...
  - rather than having a test case for multiple functionalities, it is better to devise separate test cases for each functionality of the system
  - different from module decomposition: program users perspective vs. developers
    - recall that a program user may also be another program
    - requires detailed specification



# Functional Testing

- Functional testing techniques in brief:
  - input: ITF specification
  - output: test cases specification
- Core of the methodology: partitioning the possible behaviors of the program into a finite number of homogeneous classes
  - not an actual partition, as they may overlap
  - “homogeneous” in a broad sense, depends on the program
  - often requires to integrate program specifications, good for project documentation!
- Human effort required, similar to modeling in model checking
  - in few cases, if program specifications are already formal, the work is easier
  - e.g., a model checking specification may be directly translated in test cases



# Functional Testing

- A function with two 32-bit integers has  $2^{64} \approx 10^{21}$  possible different inputs
- Given budget limitations, only an extremely tiny fraction of inputs may be tested
  - limitations are both in money and time
- Random sampling: choose test cases from a random distribution
  - of course, depending on the program specifications
  - e.g., for a function taking 3 floating points and a string, we sample from  $\mathbb{R}^3 \times A^*$ , if  $A$  is the alphabet
- To do: build a program that generate test cases by sampling the given input space
  - by definition of test case, this must also include a function to check the result

# Random Testing

- Suppose that we have to test an ITF with 2 inputs: an integer  $i$  and a floating point  $f$
- Suppose that testing budget allows testing to last  $T$  seconds, and that each run of the ITF requires  $t$  seconds: then,  $R = \lfloor \frac{T}{t} \rfloor$  runs are allowed
  - we are postponing the problem of checking the result
- Example of test case specification: for each variable,  $S = \lfloor \sqrt{R} \rfloor$  independent and equally spaced samples are taken
  - for  $i$ , take all values from  $\mathcal{I} = \{m + jl \mid j = 0, \dots, S - 1\}$ , being  $m$  ( $M$ ) the minimum (maximum) value for  $i$  and  $l = \lfloor \frac{M-m}{S} \rfloor$
  - analogous for  $f$ , defining set  $\mathcal{F}$
  - take all values from  $\mathcal{I} \times \mathcal{F}$  for testing
  - very rough, extremely huge gaps, no functional specification taken into account



# Random Testing

- Make it random: use some  $S' \gg S$ , e.g.,  $S' = kS$  with  $k = 100$ 
  - thus obtaining  $\mathcal{I} = \{m + jl \mid j = 0, \dots, S' - 1\}$ , being  $m$  ( $M$ ) the minimum (maximum) value for  $i$  and  $l = \lfloor \frac{M-m}{S'} \rfloor$
  - then, choose at random  $S$  (different) elements from  $\mathcal{I}$ , obtaining  $\mathcal{I}'$
  - analogous for  $\mathcal{F}' \subseteq \mathcal{F}$
  - take all values from  $\mathcal{I}' \times \mathcal{F}'$  for testing
  - much better, no huge gaps (simply increase  $k$ ), but still does not consider ITF specification
- What about variable-length arguments, e.g., we also have a string  $s$  as a third parameter?
  - to start with,  $S = \lfloor \sqrt[3]{R} \rfloor$
  - again, use  $S' = kS$  with  $k > 1$
  - first decide some maximum length  $M$ , then take  $S$  values from  $\mathcal{S}' = \{\text{RandomStr}(jl) \mid j = 0, \dots, S' - 1\}$ , being  $l = \lfloor \frac{M}{S'} \rfloor$  and  $\text{RandomStr}(d)$  a function creating a string of size  $d$  with random printable characters

# From Pure Random Sampling to Partitioning

- Simply random is not a good choice, better a kind of “guided” random
- Best way to guide is perform *partitioning* of input space
  - not an actual partition: the union is the whole, but partitions may have some non-null intersection
  - however, “partitioning” is standard terminology for testing
- Typical desired property: there does not exist a partition containing both failure and non-failure inputs
- In fact, by random sampling from each partition, we will for sure consider all failure inputs
  - partition of failure inputs only → some failure will be detected
- Of course, the property is desirable but impossible to obtain in the general case



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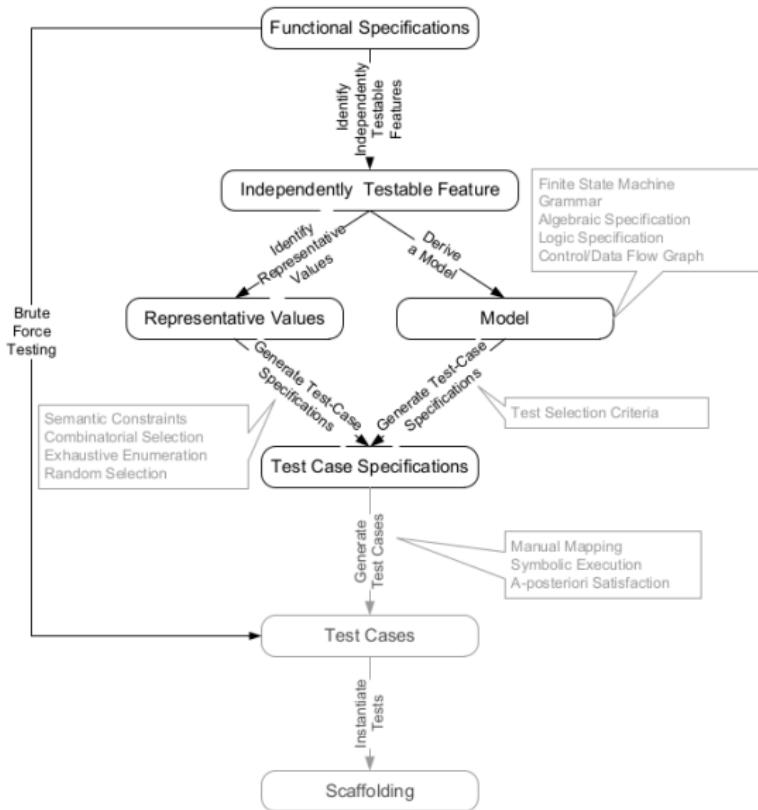
# Partition Testing

- *Partition testing*: any method that partition the input spaces in a finite number of partitions as seen above
- *Functional testing*: partition testing where the partition algorithm is based on the program specification
  - also called *specification-based partition testing*
- Generating test cases is more expensive: we also have to guarantee they belong to partitions
  - pure random does not check this, thus it is simpler
- Fewer test cases generated in the same amount of money and time
- However, it is typically more effective in finding failures



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# A Systematic Approach for Functional Testing



# A Systematic Approach for Functional Testing

- For each ITF identified, a number of inputs are needed
  - e.g., a registration on a Web page (single ITF) needs name, surname, age, ...
  - in some cases, some input may be hidden and must be explicited
    - e.g., when checking if some name is in a database, the input is not only the name, but also the database!
- Note that inputs may be grouped, but here we consider them *flattened*
  - we are in unit testing, and a method takes an instance of a class A as input? recursively consider all members of A
  - till when we are in basic data types: numbers, characters and strings



# More on Flattenization

- To flatten a class, the constructor method must be considered
  - if more than one constructor is present, consider the one with most arguments
  - if no constructor is present, this typically denotes some flaw
  - to go on anyway, directly consider class members
  - if no class member, why pass it as an argument? there should be a flaw, or it may be neglected
- Recursively flatten each constructor argument
  - till when we are in basic data types: numbers (including enumerations and booleans...), characters and strings
- Arrays may be considered as one argument
  - methodologies will typically operate on each element separately
  - this includes recursive classes or structures representing lists
    - e.g., `ArrayList` in Java



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# A Systematic Approach for Functional Testing

- For each inputs identified, a choice is needed between:
  - identify representative values
    - meaningful fixed values for inputs are directly enumerated
  - build a model
    - some model is built which generates values for input
    - e.g., a grammar may be built, defining the valid values
    - also an algorithm could be written
    - or a methodology may be used, as we will do in the following:  
Category-Partition and Catalog-based techniques
- Both methods try to detect “good” partitions for the state space



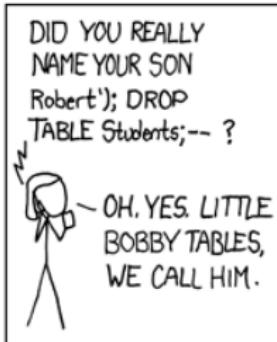
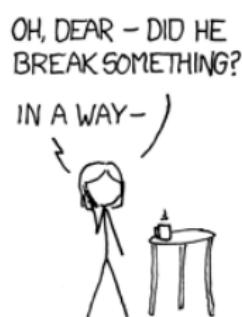
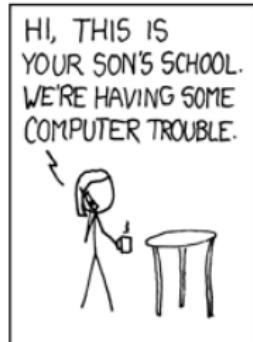
# A Systematic Approach for Functional Testing

- Combine the values of the different inputs involved
  - if all of them have been enumerated in the previous step, the Cartesian product may be used
  - however, this works for few inputs with few values, as the size explodes
  - e.g., 6 inputs with 6 values each results in about 50k tests
- Thus, we need something more clever:
  - detect illegal combinations
  - select a practical and meaningful subset of legal combinations
- Example: 2 input numbers representing length of a string and number of special characters
  - the 0 length + more than 1 special character is illegal



# Illegal Combinations: What To Do?

- It could be straightforward to think that illegal combinations of inputs must be always ruled out
- However, illegal combinations often have to be tested as well
- We may consider two possible cases:
  - the ITF is for the “general public”
  - the ITF is an API, to be invoked by programs
- As for case 1, illegal combinations should always be tested



# Illegal Combinations: What To Do?

- We may consider two possible cases:
  - ① the ITF is for the “general public”
  - ② the ITF is an API, to be invoked by programs
- As for case 1, illegal combinations should always be tested
  - generic users may easily feed “wrong” inputs
  - an error must be returned, not a failure!
- As for case 2, it depends
  - if the ITF is for internal use only, and some assurance of compliance is present from the specifications, we may rule out the illegal combination
  - otherwise, generic programs may be as generic users...
- *Fuzzing*: illegal combinations for system testing, we will be back on this



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# A Systematic Approach for Functional Testing

- General techniques reducing Cartesian products do not exist
- Insights may be present in the documentation/specification
- Typical strategies include:
  - considering a subset of each ITF
  - considering exhaustive combinations only for selected pairs
- The output is a test case specification, but may also be directly a test case
  - also an algorithm could be viewed as a test case specification
- Finally, generate the test case and instantiate (i.e., run) it
  - select one or more test cases for each test case specification
  - scaffolding for the actual run, we will be back on this



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# Combinatorial Testing

- Describes the methodologies to obtain the general approach for functional testing described above
- Two main techniques may be employed
  - Category-Partition Testing
  - Catalog-Based Testing
- A third technique only deals with the combinatorial part, thus may be applied to both: Pairwise Combination Testing



# Category-Partition Testing

- Suppose we have selected an ITF and one (flattened!) parameter of such ITF
- We have to list all of its *categories*
  - some characteristic which may differentiate among possible inputs for that parameter
  - e.g.: for a string, its length, or the number of special characters
  - e.g., for an integer, being positive or negative
  - categories may be defined also for combinations of parameters (*environmental conditions*)
  - e.g.: for a parameter string (pattern) to be found in a text: number of occurrences
  - in some cases, the “expected result” category could be added



# Category-Partition Testing

- Then, we *partition* each category into *choices*
  - in the testing sense: different partitions may have non-empty intersections
- This is done by providing general and concise rules to each category
  - e.g., the length of a string may be 0, 1, between 5 and 20, greater than 50
  - e.g., an integer may be negative, 0 or strictly positive
- Defining and using *properties* might help for impossible combinations
  - e.g., if the length of a string is 0 the property may be “property:Empty”
  - e.g., if the number of special characters is 1, it may be applied only “if:NonEmpty”

# Collapsing Spaces Example

```
public static String collapseSpaces(String argStr)
{
    char last = argStr.charAt(0);
    StringBuffer argBuf = new StringBuffer();

    for (int cldx = 0 ; cldx < argStr.length(); cldx++)
    {
        char ch = argStr.charAt(cldx);
        if (ch != ' ' || last != ' ')
        {
            argBuf.append(ch);
            last = ch;
        }
    }

    return argBuf.toString();
}
```



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# Collapsing Spaces Example

We have a function taking one string  $s$  as an input and returning a string  $s'$  as an output.

Informally:  $s'$  is the same as  $s$ , but *consecutive* spaces are collapsed into one space.

Formally: let  $S = \{(i, k) \mid s_i = ' ' \wedge (i > 1 \rightarrow s_{i-1} \neq ' ') \wedge k > 1 \wedge \wedge_{n=1}^{k-1} s_{i+n} = ' '\}$ . Let

$S' = \{(j, k) \mid \exists (i, k) \in S \wedge j = i - \sum_{(i', k) \in S \mid i < i'} (k - 1)\}$ . Let  $\sigma(S, j) = \sum_{(i, k) \in S \mid i < j} (k - 1)$ .

Then, for all  $j = 1, \dots, |s| - \sum_{(i, k) \in S} (k - 1)$ ,  $s'_j = s_{j + \sigma(S', j)}$



# Collapsing Spaces Example: Category Partition Testing

- Suppose we are performing black-box unit testing; in such a case, we are forced to consider this function as an ITF
  - inputs are already identified: exactly one string
  - thus, no problems for combinations...
- Let us begin with the characteristics of our lone input (*categorization phase*)
  - length
  - number of spaces
  - number of occurrences of consecutive spaces
  - expected result
  - min and max number of consecutive spaces
  - number of consecutive starting/trailing spaces
  - number of special characters
  - spaces only
- For the *partitioning phase*, see `cases-collapse.xls`



# $k$ -Collapsing Spaces Example

We have a function taking one string  $s$  and an integer  $n \geq 2$  as an input and returning a string  $s'$  as an output.

Informally:  $s'$  is the same as  $s$ , but  $k$  consecutive spaces, s.t.  $k \geq n$ , are collapsed into one space.

Formally: let  $S = \{(i, k) \mid s_i = ' ' \wedge (i > 1 \rightarrow s_{i-1} \neq ' ') \wedge k \geq n \wedge \wedge_{n=1}^{k-1} s_{i+n} = ' '\}$ . Let

$S' = \{(j, k) \mid \exists (i, k) \in S \wedge j = i - \sum_{(i', k) \in S \mid i < i'} (k - 1)\}$ . Let  $\sigma(S, j) = \sum_{(i, k) \in S \mid i < j} (k - 1)$ .

Then, for all  $j = 1, \dots, |s| - \sum_{(i, k) \in S} (k - 1)$ ,  $s'_j = s_{j + \sigma(S', j)}$



# $k$ -Collapsing Spaces Example: Category Partition Testing

- For the Category-Partition, let us begin with the characteristics of the input  $k$  ( $s$  is as in the previous example)
  - interval
  - domain
    - if the input is provided via a GUI, it could be not an integer...
- We also have *environmental* characteristics, i.e., which look at both inputs
  - number of  $k$  consecutive spaces occurring in  $s$
  - expected result
- For the *partitioning phase*, see `cases_collapse_k.xls`



# Roots of a 2nd Degree Equation

```
class Roots {  
    double root_one, root_two;  
    int num_roots;  
    public Roots(double a, double b, double c) {  
        double q;  
        double r;  
        // Apply the textbook quadratic formula:  
        // Roots =  $-b + \sqrt{b^2 - 4ac}$  /  $2a$   
        q = b*b - 4*a*c;  
        if (q > 0 && a != 0) {  
            // If  $b^2 > 4ac$ , there are two distinct roots  
            num_roots = 2;  
            r = (double) Math.sqrt(q);  
            root_one = ((-b) + r)/(2*a);  
            root_two = ((-b) - r)/(2*a);  
        } else if (q==0) { // (BUG HERE)  
            // The equation has exactly one root  
            num_roots = 1;  
            root_one = (-b)/(2*a);  
            root_two = root_one;  
        } else {  
            // The equation has no roots if  $b^2 < 4ac$   
            num_roots = 0;  
            root_one = -1;  
            root_two = -1;  
        }  
    }  
    public int num_roots() { return num_roots; }  
    public double first_root() { return root_one; }  
    public double second_root() { return root_two; }  
}
```



# Roots of a 2nd Degree Equation

We have a function taking three floating point numbers  $a, b, c$ . It returns three floating point numbers  $n, r_1, r_2$ .

Formally:  $n$  is the number of roots of the equation  $ax^2 + bx + c = 0$ . If  $n = 1$ , then  $r_1 = r_2$  is the root, if  $n = 2$  then  $r_1 > r_2$  are the two roots, if  $n = 0$  then  $r_1 = r_2 = -1$ .

With details: let  $R = \{x \in \mathbb{R} \mid ax^2 + bx + c = 0\}$  and  $\Delta = b^2 - 4ac$ . Then,  $n = |R|$ . Furthermore, for  $\Delta = 0$ ,  $n = 1$  and  $R = \{\xi\}$ ,  $r_1 = r_2 = \xi$ . Furthermore, for  $\Delta > 0$ ,  $n = 2$  and  $R = \{\xi_1, \xi_2\}$ ,  $r_1 = \xi_1$ ,  $r_2 = \xi_2$  with  $r_1 > r_2$ . Finally, for  $\Delta < 0$ ,  $n = 0$ ,  $R = \emptyset$  and  $r_1 = r_2 = -1$ .



# Roots of a 2nd Degree Equation: Category Partition Testing

- For the Category-Partition, let us begin with the characteristics of our three inputs separately (*categorization phase*)
  - interval
  - domain
  - validity
- As for the environment:
  - interval for  $\Delta$
- For the *partitioning phase*, see `cases_roots.xls`



# Catalog-Based Testing

- Suppose we have selected an ITF and its parameters
- Three steps:
  - ① Identify variables, definitions, preconditions, postconditions and operations on ITF parameters from the specification
  - ② Derive a first set of test case specifications from the items identified above
  - ③ Complete the test case specifications using catalogs
- Catalogs are built over time and experience, help in identify values for a specific class
  - each software house (and developer/test engineer) has its own
  - e.g., when an integer is involved, always include a test with that integer equal to 0
- Catalog-Based Testing is a good technique also without catalogs
  - on the contrary, using catalog only may not be a good idea
  - catalogs may also be used in Category-Partition Testing

# Catalog Example

## Boolean

- [in/out] True
- [in/out] False

## Enumeration

- [in/out] Each enumerated value
- [in] Some value outside the enumerated set

## Range $L \dots U$

- [in]  $L - 1$  (the element immediately preceding the lower bound)
- [in/out]  $L$  (the lower bound)
- [in/out] A value between  $L$  and  $U$
- [in/out]  $U$  (the upper bound)
- [in]  $U + 1$  (the element immediately following the upper bound)

## Numeric Constant $C$

- [in/out]  $C$  (the constant value)
- [in]  $C - 1$  (the element immediately preceding the constant value)
- [in]  $C + 1$  (the element immediately following the constant value)
- [in] Any other constant compatible with  $C$

## Non-Numeric Constant $C$

- [in/out]  $C$  (the constant value)
- [in] Any other constant compatible with  $C$
- [in] Some other compatible value

## Sequence

- [in/out] Empty
- [in/out] A single element
- [in/out] More than one element
- [in/out] Maximum length (if bounded) or very long
- [in] Longer than maximum length (if bounded)
- [in] Incorrectly terminated

## Scan with action on elements $P$

- [in]  $P$  occurs at beginning of sequence
- [in]  $P$  occurs in interior of sequence
- [in]  $P$  occurs at end of sequence
- [in]  $PP$  occurs contiguously
- [in]  $P$  does not occur in sequence
- [in]  $pP$  where  $p$  is a proper prefix of  $P$
- [in] Proper prefix  $p$  occurs at end of sequence



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# Identify Elementary Items of the Specification

- From initial specification of a unit to elementary items of basic types:

**Preconditions** conditions on input which must be true before invoking the unit test

- may be checked by the unit itself (*validated preconditions*)...
- or by the outside caller (*assumed preconditions*)

**Postconditions** result of execution

**Variables** input, output or intermediate

**Operations** performed on input and/or intermediate values

**Definitions** shorthands in the specification



# Derive a First Set of Test Case Specifications

- We want to partition the input domain, and we use the previously collected information for this purpose
  - for each validated precondition  $P$ , we have two classes of inputs: inputs in which  $P$  holds, and inputs in which  $P$  does not hold
    - a single validated precondition may be split in two or more parts, if it involves ANDs or ORs
  - for each assumed precondition  $P$ , we only consider input satisfying  $P$ 
    - otherwise, unit behaviour is typically undefined
  - if a postcondition has a guard, consider the guard as a validated precondition
  - if a definition involving variables has a guard, consider the guard as a validated precondition



# Complete Test Case Specifications Using Catalogs

- Generate additional test case specifications from variables and operations
- This is done using a pre-existing catalog, to be sequentially scanned:
  - for each catalog entry, analyze all elementary items and possibly add cases
- A catalog is typically organized with an entry for each type of variable or operation
- Inside each entry, a distinction is made between input, output or input/output variables
- Then, a suggestion on values to be considered is provided
- Different catalogs may be used by different companies
  - also, in the same company for different application domains



# Collapsing Spaces Example

```
public static String collapseSpaces(String argStr)
{
    char last = argStr.charAt(0);
    StringBuffer argBuf = new StringBuffer();

    for (int cldx = 0 ; cldx < argStr.length(); cldx++)
    {
        char ch = argStr.charAt(cldx);
        if (ch != ' ' || last != ' ')
        {
            argBuf.append(ch);
            last = ch;
        }
    }

    return argBuf.toString();
}
```



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# Collapsing Spaces Example

We have a function taking one string  $s$  as an input and returning a string  $s'$  as an output.

Informally:  $s'$  is the same as  $s$ , but *consecutive* spaces are collapsed into one space.

Formally: let  $S = \{(i, k) \mid s_i = ' ' \wedge (i > 1 \rightarrow s_{i-1} \neq ' ') \wedge k > 1 \wedge \wedge_{n=1}^{k-1} s_{i+n} = ' '\}$ . Let

$S' = \{(j, k) \mid \exists (i, k) \in S \wedge j = i - \sum_{(i', k) \in S \mid i < i'} (k - 1)\}$ . Let  $\sigma(S, j) = \sum_{(i, k) \in S \mid i < j} (k - 1)$ .

Then, for all  $j = 1, \dots, |s| - \sum_{(i, k) \in S} (k - 1)$ ,  $s'_j = s_{j + \sigma(S', j)}$



# Collapsing Spaces Example: Catalog-based Testing

- For the Catalog-based Testing, let us begin with the elementary items:
  - Variables
    - $s$ : input string
    - $s'$ : output string
  - Definitions
    - a “space” corresponds to ASCII code 0x20
  - Assumed Preconditions:
    - $s$  is a NULL-terminated string of characters
  - Validated Preconditions: NONE



# Collapsing Spaces Example: Catalog-based Testing

Continuing from the previous slide:

- Postconditions:
  - if  $s$  does not contain occurrences of  $n \geq 2$  consecutive spaces,  $s' = s$
  - otherwise:
    - for any two non-space characters  $a, b$  at position  $i < j$  in  $s$ , both  $a, b$  are also in  $s'$  at positions  $i' < j'$
    - the same holds for space characters, provided they are not preceded or followed by other space characters
    - for all maximal substrings of  $n \geq 2$  spaces at position  $i$  in  $s$ , there will be a single space in  $s'$  at position  $i' \leq i$
- Operations
  - scan  $s$ , searching for consecutive spaces
  - build a new string containing the result
  - modify a string by deleting some spaces inside it



# Collapsing Spaces Example: Catalog-based Testing

- We now generate test case specifications, by also specifying from where they come
  - POST1: without consecutive spaces,  $s' = s$ 
    - TC-POST1-1:  $s$  does not contain consecutive spaces
    - TC-POST1-2:  $s$  contains  $n \geq 2$  consecutive spaces
  - POST2: with consecutive spaces, in  $s'$  they are replaced by single spaces
    - we will obtain the same as before, thus we can skip
  - We are now ready to apply the catalog



# Catalog Example

## Boolean

- [in/out] True
- [in/out] False

## Enumeration

- [in/out] Each enumerated value
- [in] Some value outside the enumerated set

## Range $L \dots U$

- [in]  $L - 1$  (the element immediately preceding the lower bound)
- [in/out]  $L$  (the lower bound)
- [in/out] A value between  $L$  and  $U$
- [in/out]  $U$  (the upper bound)
- [in]  $U + 1$  (the element immediately following the upper bound)

## Numeric Constant $C$

- [in/out]  $C$  (the constant value)
- [in]  $C - 1$  (the element immediately preceding the constant value)
- [in]  $C + 1$  (the element immediately following the constant value)
- [in] Any other constant compatible with  $C$

## Non-Numeric Constant $C$

- [in/out]  $C$  (the constant value)
- [in] Any other constant compatible with  $C$
- [in] Some other compatible value

## Sequence

- [in/out] Empty
- [in/out] A single element
- [in/out] More than one element
- [in/out] Maximum length (if bounded) or very long
- [in] Longer than maximum length (if bounded)
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## Scan with action on elements $P$

- [in]  $P$  occurs at beginning of sequence
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- [in]  $P$  occurs at end of sequence
- [in]  $PP$  occurs contiguously
- [in]  $P$  does not occur in sequence
- [in]  $pP$  where  $p$  is a proper prefix of  $P$
- [in] Proper prefix  $p$  occurs at end of sequence



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# Collapsing Spaces Example: Catalog-based Testing

- “Enumeration” may be applied to the definition, thus
  - TC-DEF-1:  $s$  contains a space
    - already inside TC-POST1-2, we may skip this
  - TC-DEF-1:  $s$  does not contain a space
- Also “Non-numeric Constant” may be applied to the definition
  - TC-DEF-2:  $s$  contains a TAB
  - TC-DEF-3:  $s$  contains a CR
  - TC-DEF-4:  $s$  contains a LF
  - TC-DEF-5:  $s$  contains a CR+LF

# Collapsing Spaces Example: Catalog-based Testing

- “Sequence” may be applied to our string  $s$ , thus:
  - TC-VAR1-1:  $s$  is the empty string
  - $s$  is a string with only one character, i.e.:
    - TC-VAR1-2-1:  $s$  is a TAB
    - TC-VAR1-2-2:  $s$  is a CR
    - TC-VAR1-2-3:  $s$  is a LF
    - TC-VAR1-2-4:  $s$  is a CR+LF (ok, two characters)
    - TC-VAR1-2-5:  $s$  is a special character different from above
    - TC-VAR1-2-6:  $s$  is a non-special character
  - TC-VAR1-3:  $s$  has length  $> 1$
  - TC-VAR1-4:  $s$  has a very high length, say  $> 1000$
  - if this is an HTML page, with a limit on  $s$ , try a length greater than that limit



# Collapsing Spaces Example: Catalog-based Testing

- “Operation” may be applied to our operation, thus:
  - TC-OP-1:  $s$  begins with two spaces
  - TC-OP-2:  $s$  contains two spaces
    - might correct TC-POST1-2, so as  $n > 2$
  - TC-OP-3:  $s$  ends with two spaces
  - TC-OP-4:  $s$  contains 4 spaces
    - might correct TC-POST1-2, so as  $n > 2 \wedge n \neq 4$
  - TC-OP-5:  $s$  contains 3 spaces
    - might correct TC-POST1-2, so as  $n \geq 5$
  - TC-OP-6:  $s$  ends with one space



# $k$ -Collapsing Spaces Example

We have a function taking one string  $s$  and an integer  $n \geq 2$  as an input and returning a string  $s'$  as an output.

Informally:  $s'$  is the same as  $s$ , but  $k$  consecutive spaces, s.t.  $k \geq n$ , are collapsed into one space.

Formally: let  $S = \{(i, k) \mid s_i = ' ' \wedge (i > 1 \rightarrow s_{i-1} \neq ' ') \wedge k \geq n \wedge \wedge_{n=1}^{k-1} s_{i+n} = ' '\}$ . Let

$S' = \{(j, k) \mid \exists (i, k) \in S \wedge j = i - \sum_{(i', k) \in S \mid i < i'} (k - 1)\}$ . Let  $\sigma(S, j) = \sum_{(i, k) \in S \mid i < j} (k - 1)$ .

Then, for all  $j = 1, \dots, |s| - \sum_{(i, k) \in S} (k - 1)$ ,  $s'_j = s_{j + \sigma(S', j)}$



# $k$ -Collapsing Spaces Example: Catalog-based Testing

- Let us add elementary items for input  $k$ :
  - Add variable:  $k$ , as the input number of consecutive spaces
  - Add assumed precondition:  $k \in \mathbb{Z}$ 
    - might not be true if this is an HTML form...
  - Validated Preconditions:  $k \geq 2$
  - Postconditions (updated):
    - if  $s$  does not contain occurrences of  $n \geq k$  consecutive spaces,  $s' = s$
    - if  $s$  contains occurrences of  $n \geq k$  consecutive spaces,  $s'$  is initially equal to  $s$ , then all  $n \geq k$  consecutive spaces are replaced with one space only
  - Operations (updated):
    - scan  $s$ , searching for at least  $k$  consecutive spaces



# $k$ -Collapsing Spaces Example: Catalog-based Testing

- TC-POST1-1:  $s$  does not contain  $n \geq k$  consecutive spaces
- TC-POST1-2:  $s$  contains  $n \geq k$  consecutive spaces
- TC-POST3-1:  $k < 2$
- TC-POST3-2:  $k \geq 2$
- TC-VAR2-1:  $k = 1$
- TC-VAR2-2:  $k = 2$
- TC-VAR2-3:  $k > 2$

# Roots of a 2nd Degree Equation

```
class Roots {  
    double root_one, root_two;  
    int num_roots;  
    public Roots(double a, double b, double c) {  
        double q;  
        double r;  
        // Apply the textbook quadratic formula:  
        // Roots =  $-b + \sqrt{b^2 - 4ac}$  /  $2a$   
        q = b*b - 4*a*c;  
        if (q > 0 && a != 0) {  
            // If  $b^2 > 4ac$ , there are two distinct roots  
            num_roots = 2;  
            r = (double) Math.sqrt(q);  
            root_one = ((-b) + r)/(2*a);  
            root_two = ((-b) - r)/(2*a);  
        } else if (q==0) { // (BUG HERE)  
            // The equation has exactly one root  
            num_roots = 1;  
            root_one = (-b)/(2*a);  
            root_two = root_one;  
        } else {  
            // The equation has no roots if  $b^2 < 4ac$   
            num_roots = 0;  
            root_one = -1;  
            root_two = -1;  
        }  
    }  
    public int num_roots() { return num_roots; }  
    public double first_root() { return root_one; }  
    public double second_root() { return root_two; }  
}
```



# Roots of a 2nd Degree Equation

We have a function taking three floating point numbers  $a, b, c$ . It returns three floating point numbers  $n, r_1, r_2$ .

Formally:  $n$  is the number of roots of the equation  $ax^2 + bx + c = 0$ . If  $n = 1$ , then  $r_1 = r_2$  is the root, if  $n = 2$  then  $r_1 > r_2$  are the two roots, if  $n = 0$  then  $r_1 = r_2 = -1$ .

With details: let  $R = \{x \in \mathbb{R} \mid ax^2 + bx + c = 0\}$  and  $\Delta = b^2 - 4ac$ . Then,  $n = |R|$ . Furthermore, for  $\Delta = 0$ ,  $n = 1$  and  $R = \{\xi\}$ ,  $r_1 = r_2 = \xi$ . Furthermore, for  $\Delta > 0$ ,  $n = 2$  and  $R = \{\xi_1, \xi_2\}$ ,  $r_1 = \xi_1$ ,  $r_2 = \xi_2$  with  $r_1 > r_2$ . Finally, for  $\Delta < 0$ ,  $n = 0$ ,  $R = \emptyset$  and  $r_1 = r_2 = -1$ .



# Roots of a 2nd Degree Equation: Catalog-based Testing

- VAR1, VAR2, VAR3:  $a, b, c$
- VAR4, VAR5, VAR6:  $n, r_1, r_2$
- DEF1:  $\Delta = b^2 - 4ac$
- PRE1, PRE2, PRE3 (assumed or validated):  $a, b, c \in \mathbb{R}$
- POST1: if  $\Delta < 0$ , then  $n = 0, r_1 = r_2 = -1$
- POST2: if  $\Delta = 0$ , then  $n = 1$  and  $r_1 = r_2$  are s.t.  
 $ar_1^2 + br_1 + c = 0$
- POST3: if  $\Delta > 0$ , then  $n = 2$  and,  $\forall r \in \{r_1, r_2\}$ ,  
 $ar^2 + br + c = 0$
- OP1: compute  $\Delta$
- OP2, OP3: compute  $\frac{-b \pm \sqrt{\Delta}}{2a}$



# Roots of a 2nd Degree Equation: Catalog-based Testing

- From POST1:  $\Delta < 0, \Delta \geq 0$
- From POST2:  $\Delta = 0, \Delta \neq 0$
- From POST3:  $\Delta > 0, \Delta \leq 0$
- Thus, TC-POST-1, TC-POST-2, TC-POST-3:  
 $\Delta < 0, \Delta = 0, \Delta > 0$
- If PRE1 is validated (same for PRE2, PRE3):
  - TC-PRE1-1:  $a$  contains multiple dots
  - TC-PRE1-2:  $a$  contains multiple E
  - TC-PRE1-3:  $a$  is bigger than maximum long double (if applicable)
  - TC-PRE1-4:  $a > 0$  is lower than long double epsilon (if applicable)
  - TC-PRE1-5:  $a$  contains alphabetic characters (different from E/e)



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# Pairwise Combination Testing

- Suppose that we have a set of test cases specifications generated by Category-Partition or Catalog-based Testing
- Pure Category-Partition or Catalog-based Testing considers all possible combinations of test case specifications
- Easily, the number of resulting combinations may be intractably high
  - similar to the state space explosion problem in model checking
- Some adjustment may be performed by applying some “reasonable” constraint
- Pairwise Combination Testing offers a systematic way to cut the number of resulting combinations



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# Pairwise Combination Testing

- Suppose we have  $T_1, \dots, T_n$  “single” test cases specifications (*test factors*)
  - each test factor  $T_i$  has  $|T_i|$  different choices
  - e.g., in the collapsing spaces example, we have  $|T_{\text{length}}| = 4, |T_{\text{spaces}}| = 5, |T_{\text{occConsSp}}| = 3$
  - may also work with “raw” test cases
- Then, the number of combined test case specifications is  $\prod_{i=1}^n |T_i|$
- With pairwise combination testing, they are usually equal to  $|T_M| \cdot |T_m|$ , being  $T_m, T_M$  the two bigger sets
  - a generic formula for the size is not available
  - however, effective tools are available to generate test cases
  - see, e.g., <https://github.com/microsoft/pict>
- It has been shown that this is a *practical good solution* for testing

# Pairwise Combination Testing

- The following properties must be true for the Pairwise Testing result  $R \subseteq \prod_{i=1}^n T_i$ 
  - $\forall 1 \leq i < j \leq n, \forall (v_1, v_2) \in T_i \times T_j, \exists (w_1, \dots, w_n) \in R$  s.t.  $w_i = v_1 \wedge w_j = v_2$
  - that is: for any possible choice of two test factors, all possible pairs of values are present in the result
  - *orthogonal arrays*: all pairs are covered the same number of times
  - for  $(v_1, v_2) \in T_i \times T_j$ , let  $C(v_1, v_2) = \{(w_1, \dots, w_n) \in R \text{ s.t. } w_i = v_1 \wedge w_j = v_2\}$
  - then,  $\exists p$  s.t., for all  $(v_1, v_2) \in T_i \times T_j, |C(v_1, v_2)| = p$
- May be generalized to  $k \leq n$ 
  - consider  $k$ -tuples instead of pairs
  - $R = \prod_{i=1}^n T_i$  if only if  $n = k$
- Some Category-Partition-like constraint may still be applied on the result
  - this is what also pict allows to do

# Structural Testing

- Functional testing is mainly black-box: no need of seeing the actual software
- If the source code is available, something may be done to add some more test cases
  - not necessarily the full “program”, also some model may be sufficient
  - e.g., a control flow graph
- Typical question: did we cover all “relevant” parts of the software?



# Structural Testing

- If some statement has never been executed during all tests, that is typically not good
- This happens if the statement is executed only if  $C$  holds, and for all test cases  $C$  does not hold
  - inside an `if`, but it is not the only case
  - may be a `while`, or after a `return...`
- Of course, it may happen that a statement will never be executed at all (*unreachable code*)
- Of course, having all statements executed does not guarantee errors are caught
  - it may be the case that only given inputs trigger a failure
  - or the implementation may be faulty w.r.t. the specification, not considering some cases
  - so, structural testing typically *complements functional testing*



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# Structural Testing and Adequacy Criteria

- One major usage of structural testing is to define *adequacy criteria*
- That is: suppose we have already generated a test suite for our ITF
- Is this test suite adequate w.r.t. some measurable criteria?
- In the following, we will mainly provide definitions for meaningful criteria which exploits program source code (mainly its CFG)
- Is it possible to reverse this reasoning? That is:
  - ① we select an adequacy criterion
  - ② we generate test case specifications which pass the criterion
  - ③ we generate test cases fulfilling the test case specifications



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# Structural Testing and Adequacy Criteria

- Step 2 above is all but simple
- As an example, some adequacy criteria require to make a given condition true or false
  - a condition may be used by an if or a while
- Of course, in the general case this is an undecidable problem
  - that is: given a program and a condition inside it, make the condition be true/false
  - some of the difficulties: it may be the case that the variables are changed before arriving to the condition, thus a reverse engineering is required
  - the condition may involve a function call
  - the condition may be unreachable for the selected values
  - ...
- Human effort is required, or sub-optimal solutions must be accepted

# Statement Testing

- Faults are in statements
  - also including expression evaluations
- A fault in a statement cannot be revealed without executing the faulty statement
- A test suite  $T$  for a program  $P$  satisfies the *statement adequacy criterion* for  $P$ , iff, for each statement  $S$  of  $P$ , there exists at least one test case in  $T$  that causes the execution of  $S$ 
  - i.e., every node in the control flow graph of  $P$  is visited by some execution path exercised by a test case in  $T$
- If not all statements, let us measure how many of them:  
$$\text{statement coverage } C_S = \frac{\#\text{execd statm}}{\#\text{all statm}}$$



# Statement and Block Testing

- If the CFG is provided, then “blocks” are considered instead of “statements”
  - depending on CFG granularity
- If  $C_{Ss}(T)$ ,  $C_{Sb}(T)$  are statement and block coverage for a test suite  $T$ , and  $C_{Ss}(T_1) > C_{Ss}(T_2)$ , then  $C_{Sb}(T_1) > C_{Sb}(T_2)$ 
  - there is a kind of monotonicity
- On the other hand, test suites with fewer test cases may achieve a higher coverage than test suites with more
  - e.g., because the input is a string, so having just few long strings may be enough, whilst having many short strings may miss some statement



# How to Measure Adequacy?

- Suppose we have a code and a test suite, how can we actually measure statement coverage?
- We have to instrument the code: see `collapse_spaces.java`
- It may also be done by existing tools: e.g., CTC++
  - works for C, C++ and Java
  - commercial product, works on all platforms
  - enhanced compiler: you invoke CTC++ compiler and run the executable as many times you want
  - CTC++ additional tools are available to analyze coverages
  - not only statement coverage, also the following ones
- Very few free-to-use tools exists for code coverage instrumentation
  - jacoco for Java



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# Branch Testing

- If statement coverage is full, this means that all conditions are evaluated at least once
- However, this does not imply that all *branches* are considered
  - a branch is an edge between two blocks, traversed iff some condition holds
- That is, that all conditions are evaluated at least once true and at least once false
- In fact, an *else* may be missing, thus a perfect statement coverage test suite may not consider the condition being false
- This may be a problem in many cases



# Branch Testing

- $T$  satisfies the *branch adequacy criterion* for  $P$  iff, for each branch  $B$  of  $P$ , there exists at least one test case in  $T$  that causes execution of  $B$
- In the CFG, all edges must be exercised by some test case in  $T$
- Branch coverage ratio:  $C_B = \frac{\#\text{execd branches}}{\#\text{all branches}}$



# Condition Testing

- If conditions are composed by multiple atomic propositions, branch coverage could be not enough
  - e.g., a condition  $A \wedge B$ , with  $A$  always true, may pass the branch coverage criterion...
- Thus, we want all atomic propositions in all conditions to be evaluated at least once true and at least once false
- $T$  satisfies the *condition adequacy criterion* for  $P$  iff, for each basic condition  $C$  in  $P$ ,  $C$  has a true outcome in at least one test case and a false outcome in at least one test case in  $T$
- Cannot be directly observed in CFGs
- Basic condition coverage ratio:  $C_{BC} = \frac{\# \text{resulting truth values}}{2 \# \text{all basic conditions}}$



# Branch and Condition Testing

- We already saw that branch coverage does not imply condition coverage
- Neither the viceversa holds: for example,  $A \wedge B$  may be exercised by  $A = 1, B = 0$  and  $A = 0, B = 1$ , which is ok for condition but not for branch
- *Branch and condition adequacy criterion*: satisfied only if both condition and branch coverage are satisfied
- Both coverage ratios can be considered

# Compound Condition Testing

- A more “natural” way to deal with both branch and condition coverage
- *Compound condition adequacy criterion*: obtain the abstract evaluation tree of each expression, then each path of such tree must be covered
  - in an abstract evaluation tree (AET), internal nodes are labeled with conditions, while edges and leaves are labeled with true or false
  - it is the same as OBDDs, with conditions instead of variables
- Thus, there must be a test case specification for each path from the root to a leaf to satisfy the adequacy criterion
- In the worst case, it is exponential



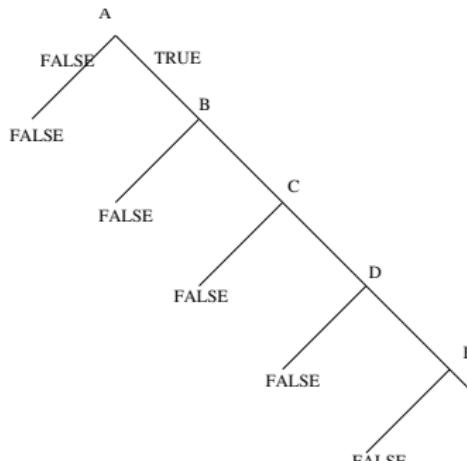
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# Compound Condition Testing: Examples

$$A \wedge B \wedge C \wedge D \wedge E$$



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# Compound Condition Testing: Examples

Compound condition for  $A \wedge B \wedge C \wedge D \wedge E$

Test Case	a	b	c	d	e
(1)	True	True	True	True	True
(2)	True	True	True	True	False
(3)	True	True	True	False	—
(4)	True	True	False	—	—
(5)	True	False	—	—	—
(6)	False	—	—	—	—



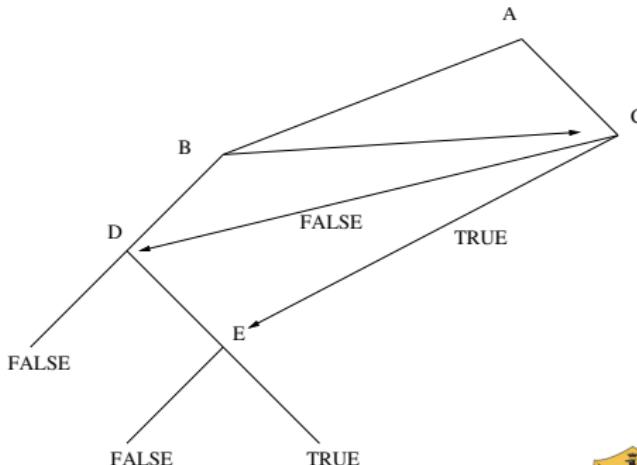
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# Compound Condition Testing: Examples

$$(((A \vee B) \wedge C) \vee D) \wedge E$$



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# Compound Condition Testing: Examples

Compound condition for  $((A \vee B) \wedge C) \vee D) \wedge E$

Test Case	a	b	c	d	e
(1)	True	–	True	–	True
(2)	False	True	True	–	True
(3)	True	–	False	True	True
(4)	False	True	False	True	True
(5)	False	False	–	True	True
(6)	True	–	True	–	False
(7)	False	True	True	–	False
(8)	True	–	False	True	False
(9)	False	True	False	True	False
(10)	False	False	–	True	False
(11)	True	–	False	False	–
(12)	False	True	False	False	–
(13)	False	False	–	False	–

# MC/DC Testing

- Compound condition may require  $2^N$  test cases, if there are  $N$  conditions
- Compound condition heavily depends on the structure itself of the condition
  - $A \wedge B \wedge C \wedge D \wedge E$  requires 6 test cases
  - $((A \vee B) \wedge C) \vee D \wedge E$  requires 13 test cases
- Modified Condition/Decision Coverage (MC/DC) overcomes this problem
- It may be proved that, if  $N$  is the number of basic conditions, then at most  $N + 1$  test cases are needed for MC/DC testing
- Thus,  $((A \vee B) \wedge C) \vee D \wedge E$  requires 6 test cases
- Can be computed automatically, given the abstract evaluation tree
- Required by many testing standards, e.g., in Aviation



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# MC/DC Testing: Definition and Properties

- *Condition*: atomic proposition
  - no boolean operators occur
  - e.g.:  $a \leq b$
- *Decision*: a whole boolean expression
  - a boolean combination of conditions
- Properties to be satisfied for the MC/DC adequacy criterion:
  - each decision in the program under test has taken all possible outcomes at least once
  - each condition in a decision has taken all possible outcomes at least once
  - each condition in a decision affects independently and correctly the outcome of this decision



# MC/DC Testing

Compound condition for  $A \wedge B \wedge C \wedge D \wedge E$

Test Case	a	b	c	d	e
(1)	True	True	True	True	True
(2)	True	True	True	True	False
(3)	True	True	True	False	—
(4)	True	True	False	—	—
(5)	True	False	—	—	—
(6)	False	—	—	—	—



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# MC/DC Testing

Compound condition for  $((A \vee B) \wedge C) \vee D \wedge E$

Test Case	a	b	c	d	e
(1)	True	–	True	–	True
(2)	False	True	True	–	True
(3)	True	–	False	True	True
(4)	False	True	False	True	True
(5)	False	False	–	True	True
(6)	True	–	True	–	False
(7)	False	True	True	–	False
(8)	True	–	False	True	False
(9)	False	True	False	True	False
(10)	False	False	–	True	False
(11)	True	–	False	False	–
(12)	False	True	False	False	–
(13)	False	False	–	False	–

# MC/DC Testing

MC/DC condition for  $((A \vee B) \wedge C) \vee D \wedge E$

	a	b	c	d	e	Decision
(1)	<u>True</u>	–	<u>True</u>	–	<u>True</u>	True
(2)	False	<u>True</u>	True	–	True	True
(3)	True	–	False	<u>True</u>	True	True
(6)	True	–	True	–	<u>False</u>	False
(11)	True	–	<u>False</u>	<u>False</u>	–	False
(13)	False	<u>False</u>	–	<u>False</u>	–	False

Each condition in a decision has taken all possible outcomes at least once → simply look at columns

Each condition in a decision affects independently and correctly the outcome of this decision → row pairs corresponding to underlined items only differs for exactly one condition (the underlined one), and the result is the opposite

# Algorithm for MC/DC Testing

```
GenMCDCCases( $D$ ) {
     $\gamma, \mathcal{C} \leftarrow \text{compoundCondition}(D);$ 
    //  $\mathcal{C}$ : set of conditions on which  $D$  depends
    ok  $\leftarrow \emptyset;$ 
    for each condition  $C \in \mathcal{C}$  {
        for each pair  $(i, j) \in |\gamma|^2, i < j$  {
            let  $r_1, r_2$  be the  $i$  and  $j$ -th row of  $\gamma$ ;
            // recall that don't cares match all
            if  $(\gamma(r_1, C) \neq \gamma(r_2, C) \wedge D(r_1) \neq D(r_2) \wedge$ 
                 $\forall C' \in \mathcal{C}. C' \neq C \rightarrow \gamma(r_1, C') = \gamma(r_2, C'))$  {
                ok  $\leftarrow$  ok  $\cup \{r_1, r_2\}$ ;
                break;
            }
        }
    }
    return  $\gamma \setminus \text{rows not in ok};$ 
}
```



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# Path Testing

- Suppose we have the CFG of a program: we may consider *paths* in it
  - starting from the root and having some finite length
  - finite length is required as testing must provide an answer at some time...
- Path adequacy criterion: for each path  $p$  of  $P$ , there exists at least one test case in  $T$  that causes the execution of  $p$
- That is, every path  $p$  is exercised by a test case in  $T$
- Path coverage is defined as  $C_P = \frac{\#\text{execd paths}}{\#\text{all paths}}$
- If the CFG has loops, the denominator is infinite, thus  $C_P = 0$ 
  - all non-trivial CFGs have loops...
- A form of path coverage may be achieved with model checking

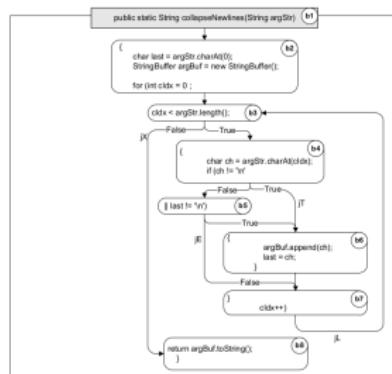


# Practical Path Coverage

- Loop boundary adequacy criterion: for each loop  $p$  in  $P$  containing a loop  $l$ , the following holds
  - in at least one execution, control reaches the loop, and then the loop control condition evaluates to False the first time it is evaluated
  - in at least one execution, control reaches the loop, and then the body of the loop is executed exactly once before control leaves the loop
  - in at least one execution, the body of the loop is repeated more than once
- Thus, we execute 0, 1 or many times the loop
- The intuition is that the loop boundary coverage criteria reflect a deeper structure in the design of a program
- Recall: in the general case, impossible to automatically generate in advance inputs fulfilling the criterion

# From CFG to LCSAJ

From	Sequence of Basic Blocks	To
entry	b1 b2 b3	jX
entry	b1 b2 b3 b4	jT
entry	b1 b2 b3 b4 b5	jE
entry	b1 b2 b3 b4 b5 b6 b7	jL
jX		b8 return
jL	b3 b4	jT
jL	b3 b4 b5	jE
jL	b3 b4 b5 b6 b7	jL



# Practical Path Coverage

- Define and exercise *sequences* of LCSAJs
  - “from” and “to” coincide
  - sequences of length 1 are almost equivalent to branch coverage (excluding some ill-based code)
- $\text{TER}_N$ , for  $N \geq 1$ , is the Test Effectiveness Ratio
  - $\text{TER}_1 = T_S$  (statements)
  - $\text{TER}_2 = T_B$  (branches)
  - $\text{TER}_{i+2} = \frac{\#\text{execd } i \text{ consecutive LCSAJs}}{\#\text{all } i \text{ consecutive LCSAJs}}$
- $\text{TER}_N = 1$  implies  $\text{TER}_i = 1$  for all  $i < N$ 
  - $\text{TER}_i$  with  $i > 3$  only required by very critical systems
- LDRAcover: commercial tool also considering LCSAJs
- Recall: in the general case, impossible to automatically generate in advance inputs exercising sequences of LCSAJs



# Practical Path Coverage

- Cyclomatic testing, based on the definition of *basis set*
  - let  $\mathcal{P}$  be the set of all paths
  - $B \subseteq \mathcal{P}$  is a basis set iff, for all  $p \in \mathcal{P}$ ,  $p$  is the concatenation of some  $q \in B$
  - it can be proved that  $|B| = e - n + 2c$ 
    - $e, n$  are number of edges and nodes
    - $c$  is the number of strongly connected components
  - for a procedure, just connect the exit back to the entry to obtain  $c = 1$  so  $|B| = e - n + 2$
  - this is the *cyclomatic complexity* of the program
- Cyclomatic testing: exercise every path in the basis set at least once



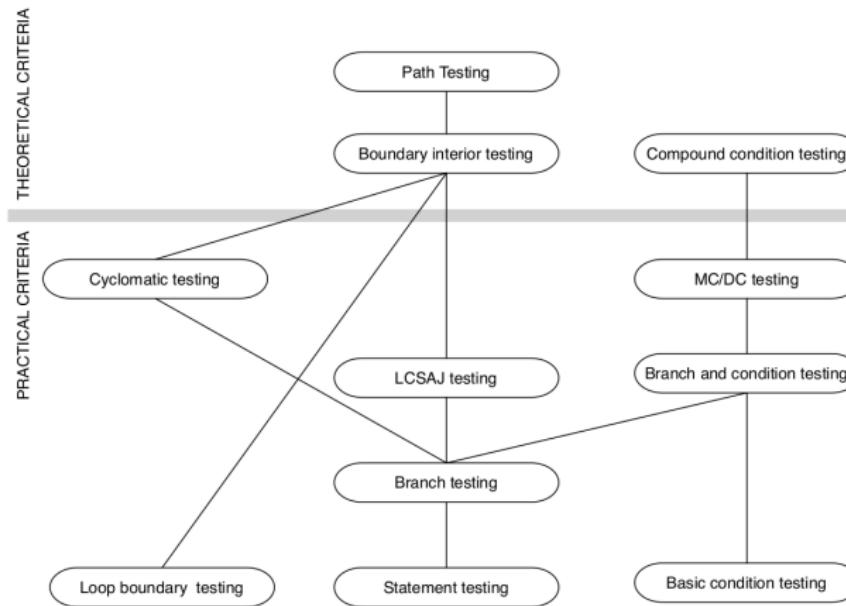
# Procedure Call Testing

- The previous techniques are ok for single procedures/functions
- When it comes to integration or system testing, it is needed to put the single pieces together
- Call coverage: exercise all different calls to *C*
  - calling the same procedure twice in different points counts as two
  - discard differences in the arguments
- Good news: if *C* is called by *A* and *B* only, and statement coverage of *A* and *B* has already been completed, then we are done!
- Bad news: for procedures with side effects, *call sequences* are important
  - especially true for object oriented programming we will be back on this



# Subsumptions

Test coverage criterion  $A$  subsumes test coverage criterion  $B$  iff, for every program  $P$ , every test set satisfying  $A$  with respect to  $P$  also satisfies  $B$  with respect to  $P$ .



# Data Flow Testing

- Again, white-box: it aids path coverage
  - paths are selected basing on how one syntactic element can affect the computation of another
  - criteria based on control structure alone fail on considering data interactions
- Computing the wrong value leads to a failure only when that value is subsequently used
- Data flow testing ensures that each computed value is actually used
- Thus, paths more likely to lead to failures are considered



# Definition-Use Associations

- Data flow testing is based on definition-use pair
  - recall: a definition writes a value in a variable, a use reads a value from a variable
  - a definition-use pair consider a definition and a following use which is not killed by another definition
- Each definition-use pair defines a definition-clear path
  - there may be several uses after the definition
- A static data flow analyzer is needed
  - for not-too-big procedures, manual instrumentation is also possible



# Data Flow Testing Criteria

- *All DU pairs adequacy criterion*: each DU pair must be exercised in at least one program execution
  - an erroneous value in a definition might be revealed only by its use
- A test suite  $T$  for a program  $P$  satisfies the all DU pairs adequacy criterion iff, for each DU pair  $(d, u)$  of  $P$ , at least one test case in  $T$  exercises  $(d, u)$
- Unsurprisingly,  $C_{DU} = \frac{\# \text{execd DU pairs}}{\# \text{all DU pairs}}$
- Finer than statement and branch coverage



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# Data Flow Testing Criteria: Example

```
14 int cgi.decode(char *encoded, char *decoded) {
15     char *eptr = encoded;
16     char *dptr = decoded;
17     int ok=0;
18     while (*eptr) {
19         char c;
20         c = *eptr;
21
22         if (c == '+') { /* Case 1: '+' maps to blank ' '
23             *dptr = ' ';
24         } else if (c == '%') { /* Case 2: '%xx' is hex for character xx */
25             int digit_high = Hex.Values[(++eptr)];
26             int digit_low = Hex.Values[(++eptr)];
27             if ( digit_high == -1 || digit_low == -1 ) {
28                 /* *dptr=? */
29                 ok=1; /* Bad return code */
30             } else {
31                 *dptr = 16* digit_high + digit_low;
32             }
33         } else { /* Case 3: All other characters map to themselves */
34             *dptr = *eptr;
35         }
36         ++dptr;
37         ++eptr;
38     }
39     *dptr = '\0';           /* Null terminator for string */
40     return ok;
41 }
```

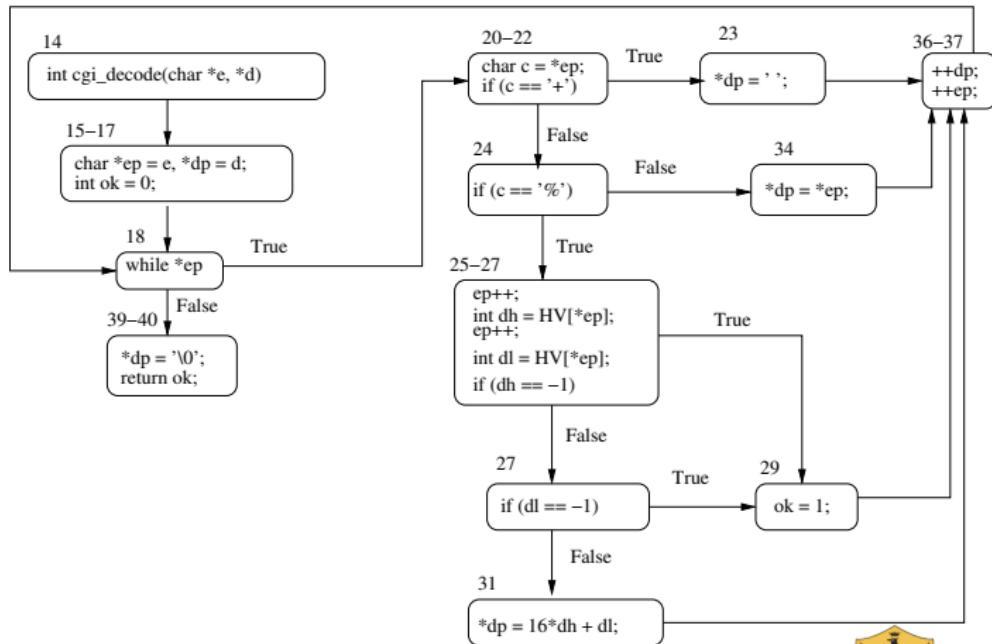


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# Data Flow Testing Criteria: Example



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# Data Flow Testing Criteria: Example

Variable	Definitions	Uses
encoded	14	15
decoded	14	16
*eptr	15, 25, 26, 37	18, 20, 25, 26, 34
eptr	15, 25, 26, 37	15, 18, 20, 25, 26, 34, 37
*dptr	16, 23, 31, 34, 36, 39	40
dptr	16, 36	16, 23, 31, 34, 36, 39
ok	17, 29	40
c	20	22, 24
digit_high	25	27, 31
digit_low	26	27, 31
Hex_Values	–	25, 26

One error: no use of \*dptr at line 40 (actually, no use at all)  
For pointers, the declaration defines both p and \*p



# Data Flow Testing Criteria: Example

List of all DU-pairs:

- encoded →  $\{(14, 15)\}$
- decoded →  $\{(14, 16)\}$
- dptr →  $\{(16, 36), (36, 36)\}$
- eptr →  $\{(26, 37), (25, 26), (15, 37), (37, 25), (15, 25), (37, 37)\}$
- \*eptr →  $\{(37, 26), (37, 25), (15, 18), (37, 34), (37, 19-20), (15, 25), (15, 26), (15, 34),$
- c →  $\{(19-20, 22), (19-20, 24)\}$   $(15, 19-20), (37, 18)\}$
- digit\_low →  $\{(26, 31), (26, 27-2)\}$
- digit\_high →  $\{(25, 27-1), (25, 31)\}$

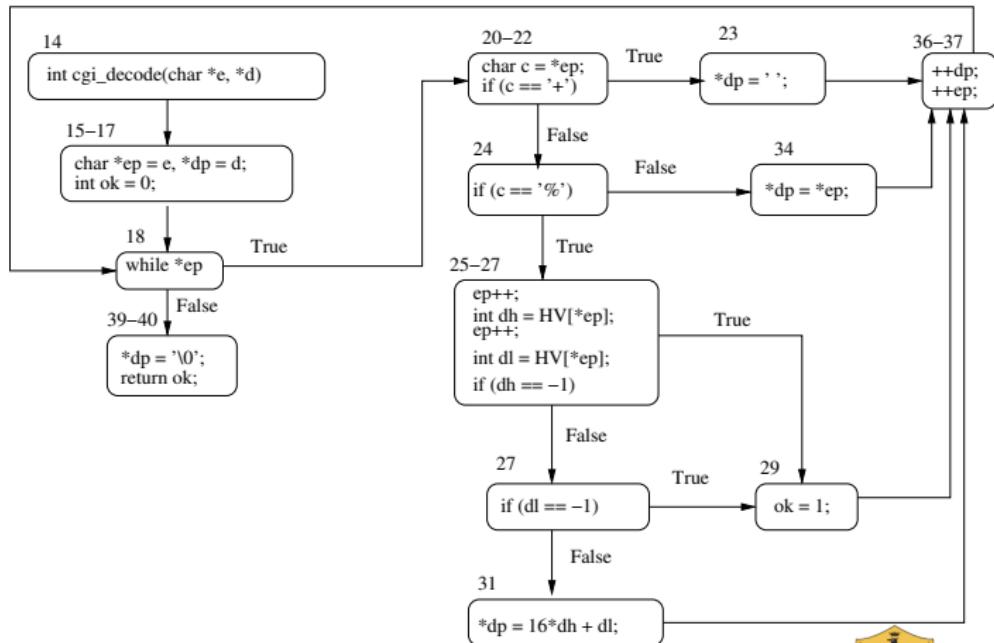


# Data Flow Testing Criteria

- *All DU paths adequacy criterion*: for each DU pair, each of the corresponding DU paths must be exercised in at least one program execution
  - if the path contains a loop, discard the loop (simple path)
- A test suite  $T$  for a program  $P$  satisfies the all DU paths adequacy criterion iff, for each DU pair  $(d, u)$  of  $P$  and simple path  $p$  from  $d$  to  $u$ , at least one test case in  $T$  exercises  $p$
- Unsurprisingly,  $C_{DUP} = \frac{\#\text{execdDU simple paths}}{\#\text{all DU simple paths}}$
- Of course, subsumes the all DU pairs coverage criterion



# All DU pairs/path: Difference



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# All DU pairs/path: Difference

- One DU pair for variable `eptr` is (15, 37)
- For the all DU-pair criterion, it is enough that at least one test case traverses both line 15 and line 37
- For the all DU-paths criterion, this is not enough as there are 2 `eptr`-definition-free paths going from 15 to 37
  - one in which the current character is +, and another in which it is neither + nor %
- Thus, there must be a test case for the first path and another for the second



# Data Flow Testing Criteria

- *All definitions adequacy criterion*: for each definition, at least one corresponding use must be exercised in at least one program execution
- A test suite  $T$  for a program  $P$  satisfies the all definitions adequacy criterion iff, for each definition  $d$  of  $P$ , there exists a DU pair  $(d, u)$  s.t. at least one test case in  $T$  exercises  $(d, u)$
- Unsurprisingly,  $C_D = \frac{\text{\#covered definition}}{\text{\#all definitions}}$
- Of course, it is subsumed by both the all DU pairs and all DU paths coverage criterion
  - all defs  $\leftarrow$  all pairs  $\leftarrow$  add paths
  - increasingly better for testing quality
    - i.e., capability of finding errors, if any
  - increasingly difficult to find values



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# Model Based Testing

- Kind of black-box testing, where specifications have some special form
  - or it is possible to extract a model from specifications
  - similar to model checking, but model is then used for testing
- Used to aid black-box approaches to identify
  - meaningful values
  - (additional) constraints
  - (additional) significant combinations
  - especially useful for integration and system testing
- Ideally, model based testing aims to generate inputs from specifications, as much as software engineer wants to generate code...



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# Model Based Testing

- Two types of models:
  - formal, i.e., with a precise syntax and semantics
    - finite state machines (usually) and grammars
    - test cases may be automatically generated
  - semiformal
    - state diagrams, class diagrams and finite state machines (sometimes)
    - automation must be used with some care



# Model Based Testing

- Models may describe:
  - input structure
    - especially for grammars
    - typically formal models, thus used to directly generate test cases
  - desired behaviour for the program, or a part of it
    - discrepancies from the model can be used as an implicit fault model to help identify boundary and error cases
- We will consider some models useful for testing
  - for each model, let us see how to generate test cases from each of them



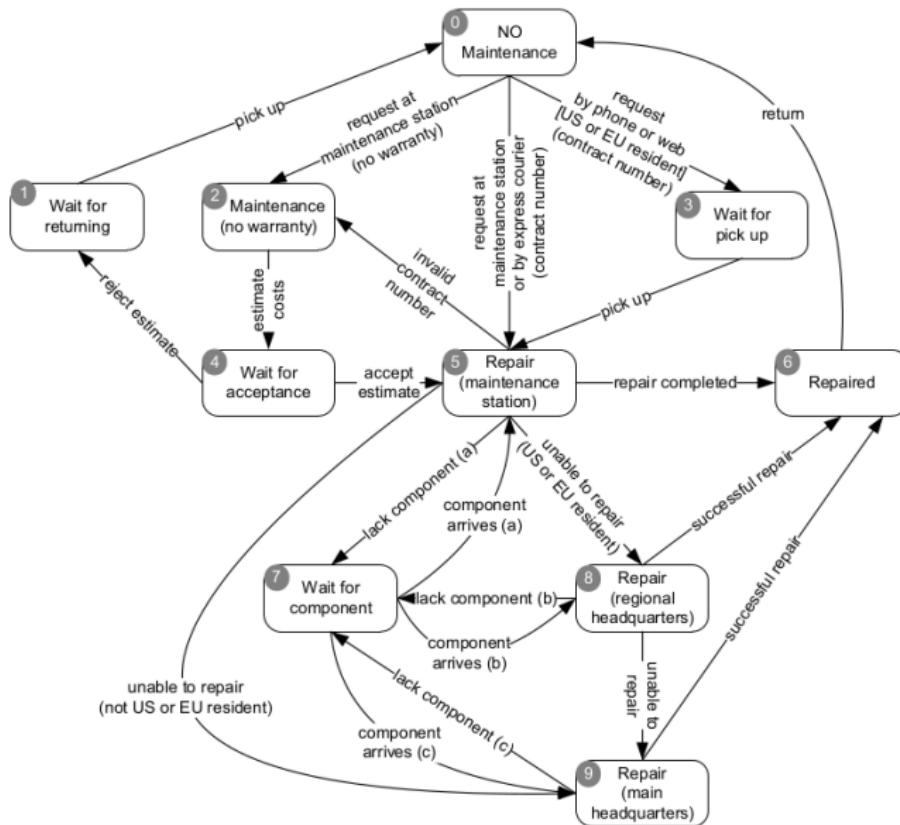
# Finite States Machines

- Common for control and reactive systems, such as
  - embedded systems (StateChart), communication protocols (SDL), menu-driven applications
  - typically multiprocess or multithread
- Many systems actually have infinite states, but often are approximable with a finite state machine as well
  - for real, a port receiving a string message should have infinite states...
- Transitions are usually guarded by conditions or input events
  - conditions may be regarded as particular input events



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# Example



# Semiformal Finite States Machines

- Sometimes they are not memoryless as they should be
  - transitions from a state must only depend on the starting state
  - instead, often it depends also on the path leading to the state (memory)
  - e.g., “Wait for component” need to remember *which* component...
- Some outgoing transitions may be missing, i.e. some input is not considered from some state
- Three possible cases:
  - don't care transition, that input is impossible in that state, e.g., because of some physical constraint
  - error transition, goes to some common error-handling procedure
  - self transition
- Though they may be “completed”, also a semiformal FSS may be useful



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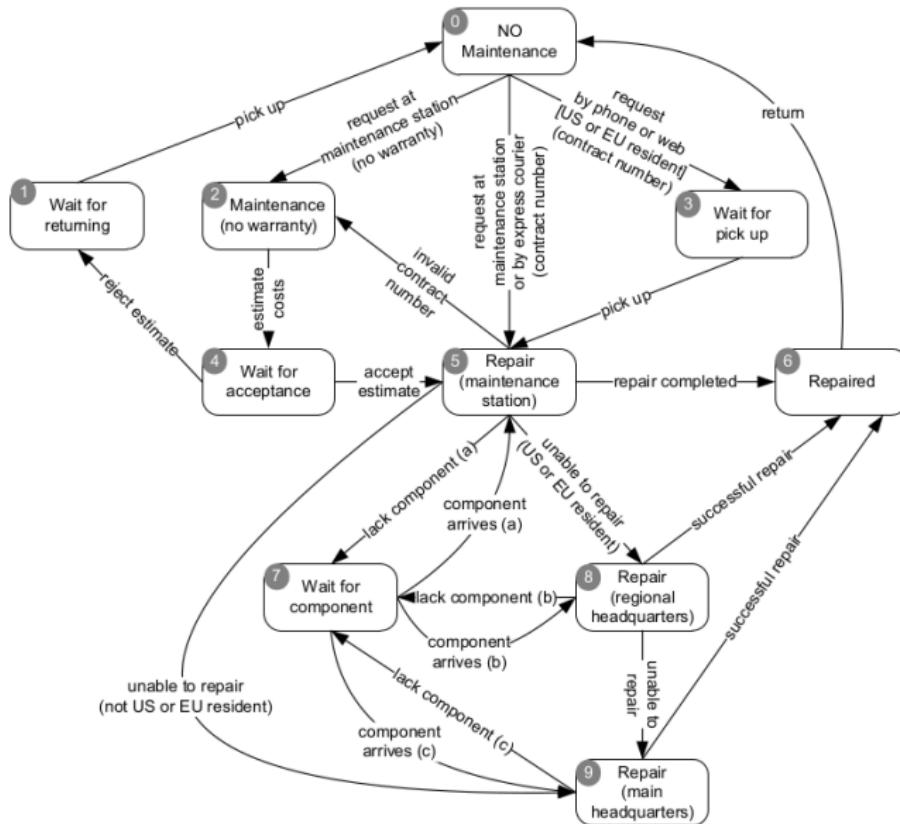
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# From Finite States Machine To Test Case Specification

- Each transition should be covered
  - could be seen as a (precondition, postcondition) pair...
- Transition coverage: all transitions are covered
- Unsurprisingly,  $C_T = \frac{\# \text{execd transitions}}{\# \text{all transitions}}$
- Looks similar to white-box testing, but here:
  - it may be applied *in advance*, thus you decide an acceptable  $C_T$ , and generate test case specifications accordingly
  - this is not directly a CFG, as it may represent something at much more higher level: ok also for integration or system testing
- Final result is test cases specifications involving transitions
  - obtaining test cases could be not simple
  - depends on the specific program under test



# Example



# Example

## T-Cover

TC-1 0 - 2 - 4 - 1 - 0  
TC-2 0 - 5 - 2 - 4 - 5 - 6 - 0  
TC-3 0 - 3 - 5 - 9 - 6 - 0  
TC-4 0 - 3 - 5 - 7 - 5 - 8 - 7 - 8 - 9 - 7 - 9 - 6 - 0

*States numbers refer to Figure 14.2. For example, TC-1 represents the path (0,2), (2,4), (4,1), (1,0).*

Though the book says it is complete, it is not: coverage is approx. 95% as transition (8, 6) is missing



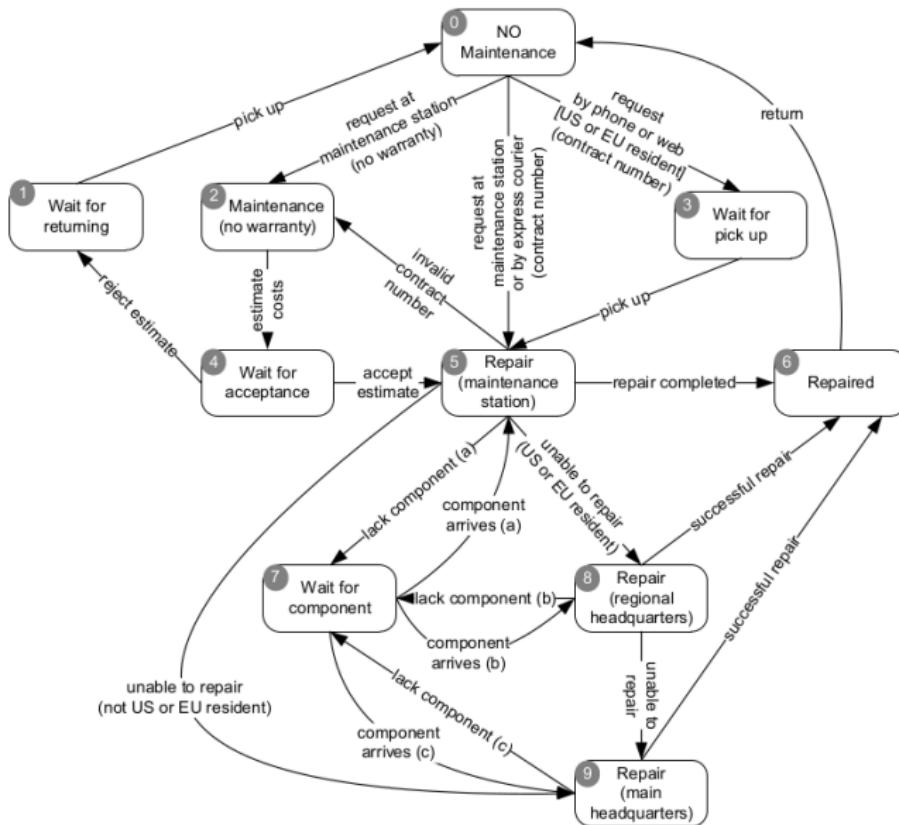
# From Finite States Machine To Test Case Specification

- For small FSS, also paths may be considered, especially if they are semiformal
  - single state path coverage criterion: all non-loop paths
  - single transition path coverage criterion: all paths in which each transition is taken just once
  - interior boundary loop coverage: for all loops, exercise the loop the minimum, the maximum, and some intermediate number of times
  - the corresponding coverage ratios may be defined
- Especially useful when states do not fully describe the system status



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## Example



# Example

<b>T-Cover</b>	
TC-1	0 – 2 – 4 – 1 – 0
TC-2	0 – 5 – 2 – 4 – 5 – 6 – 0
TC-3	0 – 3 – 5 – 9 – 6 – 0
TC-4	0 – 3 – 5 – 7 – 5 – 8 – 7 – 8 – 9 – 7 – 9 – 6 – 0

*States numbers refer to Figure 14.2. For example, TC-1 represents the path (0,2), (2,4), (4,1), (1,0).*

- single state path coverage criterion: e.g., 0-2-4-5-6 is missing
- single transition path coverage criterion: e.g., 0-2-4-1-0-5-2 is missing
- interior boundary loop coverage: e.g., 0-2-4-1-0-2-4-1 is missing



# Transition Coverage: a Possible Algorithm

- That is, an algorithm which outputs paths so that all transitions in the FSM are covered (see previous slide)
- Augmented DFS in which:
  - each time an already visited state is reached, the entire stack is output, plus the visited state
  - maintain a set of all transitions visited
  - assume you have the set of all transitions
  - stop the DFS when desired coverage is reached
- Of course, not on-the-fly, the graph is in memory in advance
  - not a problem, these are man-made (relatively) small models
  - composition between different FSMs is rarely used



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# Single State Path Coverage: a Possible Algorithm

- That is, an algorithm which outputs paths so that all non-looping paths are output
- Augmented DFS in which:
  - each time an already visited state is reached, the entire stack is saved in a set  $P$ 
    - the visited state is appended only if it is not already in the stack
  - post-process  $P$  so that  $\pi \in P$  implies  $\forall \rho \in P. \pi$  is not a prefix of  $\rho$
  - output  $P$ 
    - might stop before if coverage is already enough



# Single Transition Path Coverage: a Possible Algorithm

- That is, an algorithm which outputs paths so that all paths which do not contain the same transition twice are output
- Augmented DFS in which:
  - visited states check is replaced with visited transitions check
  - each time an already visited transition is reached, the entire stack is saved in a set  $P$ 
    - the visited transition is appended only if it is not already in the stack
  - post-process  $P$  so that  $\pi \in P$  implies  $\forall \rho \in P. \pi$  is not a prefix of  $\rho$
  - output  $P$ 
    - might stop before if coverage is already enough



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# Interior Boundary Loop Coverage: a Possible Algorithm

- That is, an algorithm which outputs 3 test cases for all looping paths: avoiding the loop, going once in the loop, going, e.g., 3 times through the loop
- Augmented DFS in which:
  - visited states check is replaced with visited transitions check
  - each time an already visited transition is reached, the entire stack is saved in a set  $P$ 
    - the visited transition is appended only if it is not already in the stack
  - post-process  $P$  so that  $\pi \in P$  implies  $\forall \rho \in P. \pi$  is not a prefix of  $\rho$
  - further post-process  $P$  so that, for each  $\pi \in P$ , the suffix for  $\pi$  which is a loop is detected
  - repeat such loop as many times as given

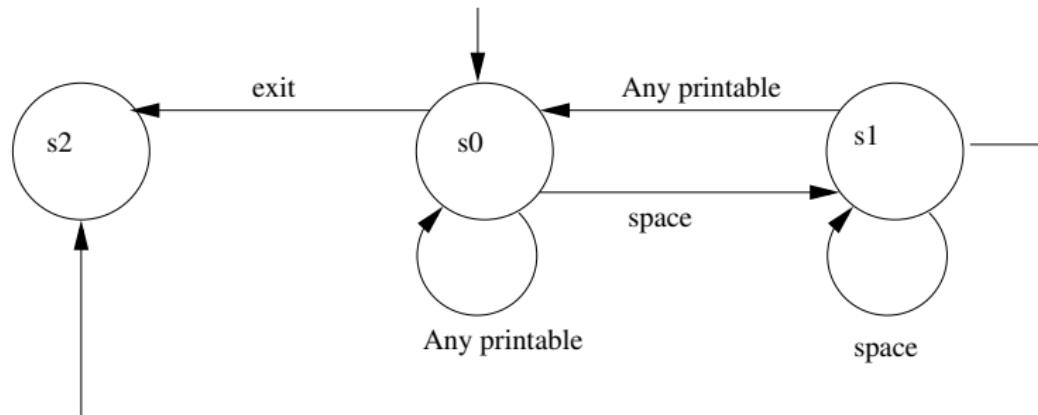


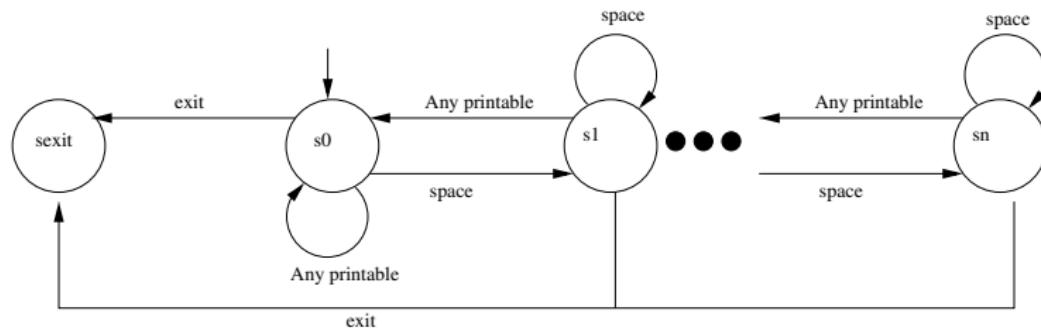
# From FSMs To Test Case Specification: A Different Perspective

- FSMs may be useful also for generating inputs values
- In this case, they are designed by the test engineers and used as a model for generating the inputs
- Useful for *sequences* of inputs, thus either:
  - strings, which includes files and DB contents
  - some software service continuously accepting inputs (e.g., controllers or servers in client-server model)
  - in this latter case, also the input timing may be output
  - could also be used online, instead of performing a pre-computation
- Alternative to Category-Partition and Catalog-Based Testing
- Similar to generating from a grammar (see below)



# Collapsing Spaces Example





- Sometimes it could be possible to derive a grammar from specifications
  - regular expressions or annotated context-free grammars (in BNF, Backus-Naur Form)
  - it could be already present as such: e.g., to describe a search pattern
  - XML schema may be easily translated into BNF
- Very good to represent inputs of varying and unbounded size, with recursive structures
- Want a test case specification? simply generate a string from the grammar!
- Similar to a walk in a graph: how to choose from many possible grammar productions?



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## Example

**Advanced search:** The *Advanced search* function allows for searching elements in the Web site database.

The key for searching can be:

**a simple string**, i.e., a simple sequence of characters

a compound string, i.e.,

- a string terminated with character \*, used as wild character, or
- a string composed of substrings included in braces and separated with commas, used to indicate alternatives

**a combination of strings**, i.e., a set of strings combined with the Boolean operators NOT, AND, OR, and grouped within parentheses to change the priority of operators.

### Examples:

**laptop** The routine searches for string “laptop”

{DVD\*,CD\*} The routine searches for strings that start with substring “DVD” or “CD” followed by any number of characters.

**NOT (C2021\*) AND C20\*** The routine searches for strings that start with substring “C20” followed by any number of characters, except substring “21.”



# Example

$\langle \text{search} \rangle ::= \langle \text{search} \rangle \langle \text{binop} \rangle \langle \text{term} \rangle \mid \boxed{\text{not}} \langle \text{search} \rangle \mid \langle \text{term} \rangle$

$\langle \text{binop} \rangle ::= \boxed{\text{and}} \mid \boxed{\text{or}}$

$\langle \text{term} \rangle ::= \langle \text{regexp} \rangle \mid \boxed{(\langle \text{search} \rangle)}$

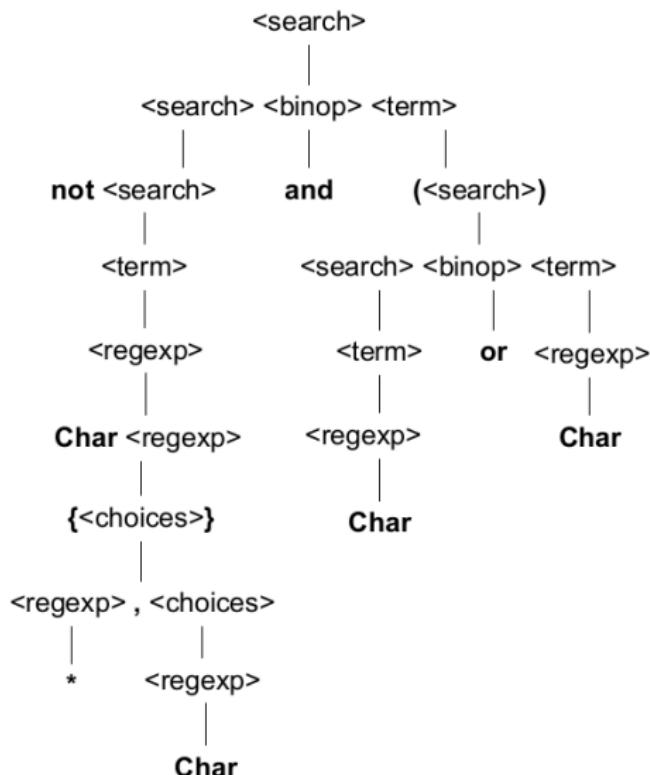
$\langle \text{regexp} \rangle ::= \text{Char} \langle \text{regexp} \rangle \mid \text{Char} \mid \boxed{\{ \langle \text{choices} \rangle \}} \mid \boxed{\star}$

$\langle \text{choices} \rangle ::= \langle \text{regexp} \rangle \mid \langle \text{regexp} \rangle \boxed{,} \langle \text{choices} \rangle$



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# Example: NOT(C2021\*) AND C20\*



# Example

```
<?xml version="1.0" encoding="ISO-8859-1" ?>
<xsd:schema xmlns:xsd="http://www.w3.org/2000/08/XMLSchema">

<xsd:annotation>
  <xsd:documentation>
    Chipmunk Computers - Product Configuration Schema
    Copyright 2001 D. Seville, Chipmunk Computers Inc.
  </xsd:documentation>
</xsd:annotation>

<xsd:element name="Model" type="ProductConfigurationType"/>

<xsd:complexType name="ProductConfigurationType">
  <xsd:attribute name="modelNumber"
    type="xsd:string" use="required"/>
  <xsd:element name="Component"
    minOccurs="0" maxOccurs="unbounded">
    <xsd:sequence>
      <xsd:element name="ComponentType" type="string"/>
      <xsd:element name="ComponentValue" type="string"/>
    </xsd:sequence>
  </xsd:element>
</xsd:complexType>
</xsd:schema>
```

# Example

$\langle Model \rangle ::= \langle modelNumber \rangle \langle compSequence \rangle \langle optCompSequence \rangle$   
 $\langle compSequence \rangle ::= \langle Component \rangle \langle compSequence \rangle \mid \boxed{\text{empty}}$   
 $\langle optCompSequence \rangle ::= \langle OptionalComponent \rangle \langle optCompSequence \rangle \mid \boxed{\text{empty}}$   
 $\langle Component \rangle ::= \langle ComponentType \rangle \langle ComponentValue \rangle$   
 $\langle OptionalComponent \rangle ::= \langle ComponentType \rangle$   
 $\langle modelNumber \rangle ::= \boxed{\text{string}}$   
 $\langle ComponentType \rangle ::= \boxed{\text{string}}$   
 $\langle ComponentValue \rangle ::= \boxed{\text{string}}$



- Productions may be different and guide the choice
  - want many short test cases? choose production with many non-terminals first
  - want few long test cases? choose production with few non-terminals first
  - of course, there are intermediate cases
- Production adequacy criterion: each production must be exercised at least once in generating the test case
  - of course,  $C_P = \frac{\# \text{execd productions}}{\# \text{all productions}}$

- Boundary condition grammar-based adequacy criterion: each production must be exercised at least  $m$  and at most  $M$  times in generating the test case
  - productions must be labeled by bounds
- Probabilistic grammar-based adequacy criterion: a probability is attached to each production
  - generation follows the given probability



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# Example

Model	$\langle Model \rangle$	$::= \langle modelNumber \rangle \langle compSequence \rangle \langle optCompSequence \rangle$
compSeq1 limit=16	$\langle compSequence \rangle$	$::= \langle Component \rangle \langle compSequence \rangle$
compSeq2	$\langle compSequence \rangle$	$::= \boxed{\text{empty}}$
optCompSeq1 limit=16	$\langle optCompSequence \rangle$	$::= \langle OptionalComponent \rangle \langle optCompSequence \rangle$
optCompSeq2	$\langle optCompSequence \rangle$	$::= \boxed{\text{empty}}$
Comp	$\langle Component \rangle$	$::= \langle ComponentType \rangle \langle ComponentValue \rangle$
OptComp	$\langle OptionalComponent \rangle$	$::= \langle ComponentType \rangle$
modNum	$\langle modelNumber \rangle$	$::= \boxed{\text{string}}$
CompTyp	$\langle ComponentType \rangle$	$::= \boxed{\text{string}}$
CompVal	$\langle ComponentValue \rangle$	$::= \boxed{\text{string}}$

# Decision Structures

- From a functional specification to a *decision table*
- Possible intermediate step: from the specification, write a Boolean formula
  - first order logic: boolean combinations of propositions
- To be done when a (part of a) specification is clearly based on some complex Boolean formula



# Decision Structures

**Pricing:** The *pricing* function determines the adjusted price of a configuration for a particular customer. The scheduled price of a configuration is the sum of the scheduled price of the model and the scheduled price of each component in the configuration. The adjusted price is either the scheduled price, if no discounts are applicable, or the scheduled price less any applicable discounts.

There are three price schedules and three corresponding discount schedules, *Business*, *Educational*, and *Individual*. The Business price and discount schedules apply only if the order is to be charged to a business account in good standing. The Educational price and discount schedules apply to educational institutions. The Individual price and discount schedules apply to all other customers. Account classes and rules for establishing business and educational accounts are described further in [...].

A discount schedule includes up to three discount levels, in addition to the possibility of “no discount.” Each discount level is characterized by two threshold values, a value for the current purchase (configuration schedule price) and a cumulative value for purchases over the preceding 12 months (sum of adjusted price).

**Educational prices** The adjusted price for a purchase charged to an educational account in good standing is the scheduled price from the educational price schedule. No further discounts apply.

**Business account discounts** Business discounts depend on the size of the current purchase as well as business in the preceding 12 months. A tier 1 discount is applicable if the scheduled price of the current order exceeds the tier 1 current order threshold, or if total paid invoices to the account over the preceding 12 months exceeds the tier 1 year cumulative value threshold. A tier 2 discount is applicable if the current order exceeds the tier 2 current order threshold, or if total paid invoices to the account over the preceding 12 months exceeds the tier 2 cumulative value threshold. A tier 2 discount is also applicable if both the current order and 12 month cumulative payments exceed the tier 1 thresholds.

**Individual discounts** Purchase by individuals and by others without an established account in good standing is based on current value alone (not on cumulative purchases). A tier 1 individual discount is applicable if the scheduled price of the configuration in the current order exceeds the tier 1 current order threshold. A tier 2 individual discount is applicable if the scheduled price of the configuration exceeds the tier 2 current order threshold.

**Special-price nondiscountable offers** Sometimes a complete configuration is offered at a special, non-discountable price. When a special, nondiscountable price is available for a configuration, the adjusted price is the nondiscountable price or the regular price after any applicable discounts, whichever is less.



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# Decision Structures

Output is “no discount” IFF

$$\begin{aligned} & ( \begin{aligned} & \text{individual account} \\ & \wedge \neg \text{ current purchase} > \text{tier 1 individual threshold} \\ & \wedge \neg \text{ special offer price} < \text{individual scheduled price} \end{aligned} ) \\ \vee \quad & ( \begin{aligned} & \text{business account} \\ & \wedge \neg \text{ current purchase} > \text{tier 1 business threshold} \\ & \wedge \neg \text{ current purchase} > \text{tier 1 business yearly threshold} \\ & \wedge \neg \text{ special offer price} < \text{business scheduled price} \end{aligned} ) \end{aligned}$$

Corresponds to fourth column in the first table and second column in the second table (next slide)



# Example

	Education		Individual						
	T	F	F	F	F	F	F	F	F
EduAc	T	T	F	F	F	F	F	F	F
BusAc	-	-	F	F	F	F	F	F	F
CP > CT1	-	-	F	F	T	T	-	-	-
YP > YT1	-	-	-	-	-	-	-	-	-
CP > CT2	-	-	-	-	F	F	T	T	T
YP > YT2	-	-	-	-	-	-	-	-	-
SP > Sc	F	T	F	T	-	-	-	-	-
SP > T1	-	-	-	-	F	T	-	-	-
SP > T2	-	-	-	-	-	F	T	-	-
<b>Out</b>	Edu	SP	ND	SP	T1	SP	T2	SP	

	Business											
	-	-	-	-	-	-	-	-	-	-	-	-
EduAc	-	-	-	-	-	-	-	-	-	-	-	-
BusAc	T	T	T	T	T	T	T	T	T	T	T	T
CP > CT1	F	F	T	T	F	F	T	T	-	-	-	-
YP > YT1	F	F	F	F	T	T	T	T	-	-	-	-
CP > CT2	-	-	F	F	-	-	-	-	T	T	-	-
YP > YT2	-	-	-	-	F	F	-	-	-	-	T	T
SP > Sc	F	T	-	-	-	-	-	-	-	-	-	-
SP > T1	-	-	F	T	F	T	-	-	-	-	-	-
SP > T2	-	-	-	-	-	F	T	F	T	F	T	
<b>Out</b>	ND	SP	T1	SP	T1	SP	T2	SP	T2	SP	T2	SP

## Constraints

at-most-one(EduAc, BusAc) at-most-one(YP < YT1, YP > YT2)

YP > YT2  $\Rightarrow$  YP > YT1 at-most-one(CP < CT1, CP > CT2)

CP > CT2  $\Rightarrow$  CP > CT1 at-most-one(SP < T1, SP > T2)

SP > T2  $\Rightarrow$  SP > T1



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# Decision Structures

## Abbreviations

EduAc	Educational account	Edu	Educational price
BusAc	Business account	ND	No discount
CP > CT1	Current purchase greater than threshold 1	T1	Tier 1
YP > YT1	Year cumulative purchase greater than threshold 1	T2	Tier 2
CP > CT2	Current purchase greater than threshold 2	SP	Special Price
YP > YT2	Year cumulative purchase greater than threshold 2		
SP > Sc	Special Price better than scheduled price		
SP > T1	Special Price better than tier 1		
SP > T2	Special Price better than tier 2		



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# Decision Structures

- A decision table directly corresponds to a Boolean formula of the form  $\wedge_{i=1}^n ((\wedge_{j=1}^m \beta_{i,j}) \rightarrow v = x_i)$ 
  - $v$  is a variable representing the output of some part of the program, and  $x_i$  the desired outcome
    - typically, some enumerated value
  - $n + 1$  columns,  $m + 1$  rows
    - first column lists all “basic conditions”  $b_1, \dots, b_m$
    - last row is for values of  $v$
    - other heading are possible to ease table understanding
  - each  $\beta_{i,j}$  is either
    - $b_i$ , if the entry  $i, j$  in the table is T
    - $\neg b_i$ , if the entry  $i, j$  in the table is F
    - void, if the entry  $i, j$  in the table is don't care
  - easy to transform in conjunctive normal form:  
$$\wedge_{i=1}^n (\vee_{j=1}^{k_i} \neg \beta_{i,j} \vee v_i = x_i)$$
  - each column  $i$  (rule) corresponds to  $\wedge_{j=1}^m \beta_{i,j} \rightarrow v_i = x_i$



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 $v_i = x_i$



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# Decision Tables

- Tables are typically augmented with *constraints*
  - other Boolean formulas on  $b_i$ , typically excluding invalid combinations
  - most typical constraint are abbreviated, e.g., *at-most-one* or *exactly one*
- Thus, the overall formula is
$$\wedge_{i=1}^n ((\wedge_{j=1}^m \beta_{i,j}) \rightarrow v = x_i) \wedge \wedge_{i=1}^k C_i$$
  - e.g., if  $C_i$  is an at-most-one( $B$ ) constraint, being  $B \subset \{\beta_1, \dots, \beta_m\}$  and  $\beta_j \in \{b_j, \neg b_j\}$ , then
$$C_i \equiv \sum_{j \mid \beta_j \in B} (\beta_j = 1) \leq 1$$
- A new table can be written by taking into account the additional constraints
  - essentially, this entails fixing some don't cares



## Example

	Education		Individual					
EduAc	T	T	F	F	F	F	F	F
BusAc	-	-	F	F	F	F	F	F
CP > CT1	-	-	F	F	T	T	-	-
YP > YT1	-	-	-	-	-	-	-	-
CP > CT2	-	-	-	-	F	F	T	T
YP > YT2	-	-	-	-	-	-	-	-
SP > Sc	F	T	F	T	-	-	-	-
SP > T1	-	-	-	-	F	T	-	-
SP > T2	-	-	-	-	-	-	F	T
Out	Edu	SP	ND	SP	T1	SP	T2	SP

E.g.: BusAc  
to F in the  
first table  
and EduAc  
to F in the  
second

	Business											
EduAc	-	-	-	-	-	-	-	-	-	-	-	-
BusAc	T	T	T	T	T	T	T	T	T	T	T	T
CP > CT1	F	F	T	T	F	F	T	T	-	-	-	-
YP > YT1	F	F	F	F	T	T	T	T	-	-	-	-
CP > CT2	-	-	F	F	-	-	-	-	T	T	-	-
YP > YT2	-	-	-	-	F	F	-	-	-	-	T	T
SP > Sc	F	T	-	-	-	-	-	-	-	-	-	-
SP > T1	-	-	F	T	F	T	-	-	-	-	-	-
SP > T2	-	-	-	-	-	-	F	T	F	T	F	T
<b>Out</b>	ND	SP	T1	SP	T1	SP	T2	SP	T2	SP	T2	SP

## Constraints

at-most-one(EduAc, BusAc)

YP > YT2  $\Rightarrow$  YP > YT1

CP > CT2  $\Rightarrow$  CP > CT1

SP > T2  $\Rightarrow$  SP > T1

at-most-one(YP < YT1, YP > YT2)

at-most-one( $CP \leq CT1$ ,  $CP \geq CT2$ )

at-most-one(SP  $\leq$  T1, SP  $\geq$  T2)



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# Decision Tables Adequacy Criteria

- *Basic condition adequacy criterion*: one test case specification for each column in the table.
  - don't cares replaced with any value, but without violating the additional constraints
  - unless the table has already been completed
- *Compound condition adequacy criterion*: one test case specification for each combination of truth values of basic conditions
  - entails  $2^m$  test cases specification, only for small tables
  - recall:  $m$  is the number of table rows
  - table is used only to compute the corresponding output value



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# Decision Tables Adequacy Criteria

- *Modified Condition/Decision Criterion (MC/DC)*
  - similar, but not the same to the structural approach with the same name
  - indeed, it cannot be the same as the result is not a boolean...
- First, some new columns must be added to the original table so that:
  - for each column  $c$  and for each  $b_i$  in  $c$  which is not don't care, obtain a new column equal to  $c$ , but where  $b_i$  is negated w.r.t.  $c$ 
    - only one value changes
  - if the new column is already present (also considering don't cares) do not add it, but replace don't cares with values from the new column, if any
  - if it is not present, the result is some error
- Finally, one test case specification for each resulting column
  - similar to the basic condition, but on the augmented table
- If some new column is added, then something was wrong with the specification, good to test

# Example

	Education		Individual						
	T	F	F	F	F	F	F	F	F
EduAc	T	T	F	F	F	F	F	F	F
BusAc	-	-	F	F	F	F	F	F	F
CP > CT1	-	-	F	F	T	T	-	-	-
YP > YT1	-	-	-	-	-	-	-	-	-
CP > CT2	-	-	-	-	F	F	T	T	T
YP > YT2	-	-	-	-	-	-	-	-	-
SP > Sc	F	T	F	T	-	-	-	-	-
SP > T1	-	-	-	-	F	T	-	-	-
SP > T2	-	-	-	-	-	F	T	-	-
<b>Out</b>	Edu	SP	ND	SP	T1	SP	T2	SP	

	Business											
	-	-	-	-	-	-	-	-	-	-	-	-
EduAc	-	-	-	-	-	-	-	-	-	-	-	-
BusAc	T	T	T	T	T	T	T	T	T	T	T	T
CP > CT1	F	F	T	T	F	F	T	T	-	-	-	-
YP > YT1	F	F	F	F	T	T	T	T	-	-	-	-
CP > CT2	-	-	F	F	-	-	-	-	T	T	-	-
YP > YT2	-	-	-	-	F	F	-	-	-	-	T	T
SP > Sc	F	T	-	-	-	-	-	-	-	-	-	-
SP > T1	-	-	F	T	F	T	-	-	-	-	-	-
SP > T2	-	-	-	-	-	F	T	F	T	F	T	
<b>Out</b>	ND	SP	T1	SP	T1	SP	T2	SP	T2	SP	T2	SP

## Constraints

at-most-one(EduAc, BusAc) at-most-one(YP < YT1, YP > YT2)

YP > YT2  $\Rightarrow$  YP > YT1 at-most-one(CP < CT1, CP > CT2)

CP > CT2  $\Rightarrow$  CP > CT1 at-most-one(SP < T1, SP > T2)

SP > T2  $\Rightarrow$  SP > T1



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# Example: Augmented Table

EduAc	T	T	F	F	F	F	F	F	F	F	F	F	F	F	F
BusAc	F	F	F	F	F	F	F	T	T	T	T	T	T	T	T
CP > CT1	T	T	F	F	T	T	T	F	F	T	F	F	F	F	T
YP > YT1	F	-	F	-	-	F	T	T	F	F	F	T	T	T	T
CP > CT2	F	F	F	F	F	F	T	T	F	F	F	F	F	F	F
YP > YT2	-	-	-	-	-	-	-	-	-	-	-	-	F	F	F
SP > Sc	F	T	F	T	F	T	-	-	F	T	F	-	F	T	-
SP > T1	F	T	F	T	F	T	F	T	F	T	F	T	F	T	F
SP > T2	F	-	F	-	F	-	F	T	F	-	F	-	F	-	F
<b>Out</b>	Edu	SP	ND	SP	T1	SP	T2	SP	ND	SP	T1	SP	T1	SP	T2

EduAc	F	F	F	F	F	T	T	T	T	F	-				
BusAc	T	T	T	T	T	F	F	F	F	F	F	F	F	F	F
CP > CT1	T	T	T	F	F	F	F	T	-	-	-	-	F		
YP > YT1	T	F	F	T	T	T	-	-	-	-	T	T			
CP > CT2	F	T	T	F	F	F	F	T	T	F	F	F			
YP > YT2	F	-	-	T	T	F	-	-	-	-	T	F			
SP > Sc	T	-	T	-	T	F	T	-	-	-	-	-	-		
SP > T1	T	F	T	F	T	F	-	-	T	T	T	T			
SP > T2	T	F	T	F	T	F	F	T	T	T	T	-			
<b>Out</b>	SP	T2	SP	T2	SP	Edu	SP	Edu	SP	SP	SP	SP			

Many errors, but gives the idea



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# Control (or Data) Flow Graphs

- Sometimes it could be possible to derive a control flow graph from specifications
  - often with coarse granularity, e.g., nodes are single computations or computation steps
  - example: interactions with a database
  - as opposed to before, where CFG is extracted from code
  - closer to implementation than state diagrams, e.g., multiple outgoing edges are typically either true or false, or some enumeration from a switch
- The statement adequacy criterion becomes node adequacy criterion
- The branch adequacy criterion does not change name
- Other criteria seen for code control flow graphs may be applied as well
  - however, statement and branch are usually *ok at this* granularity



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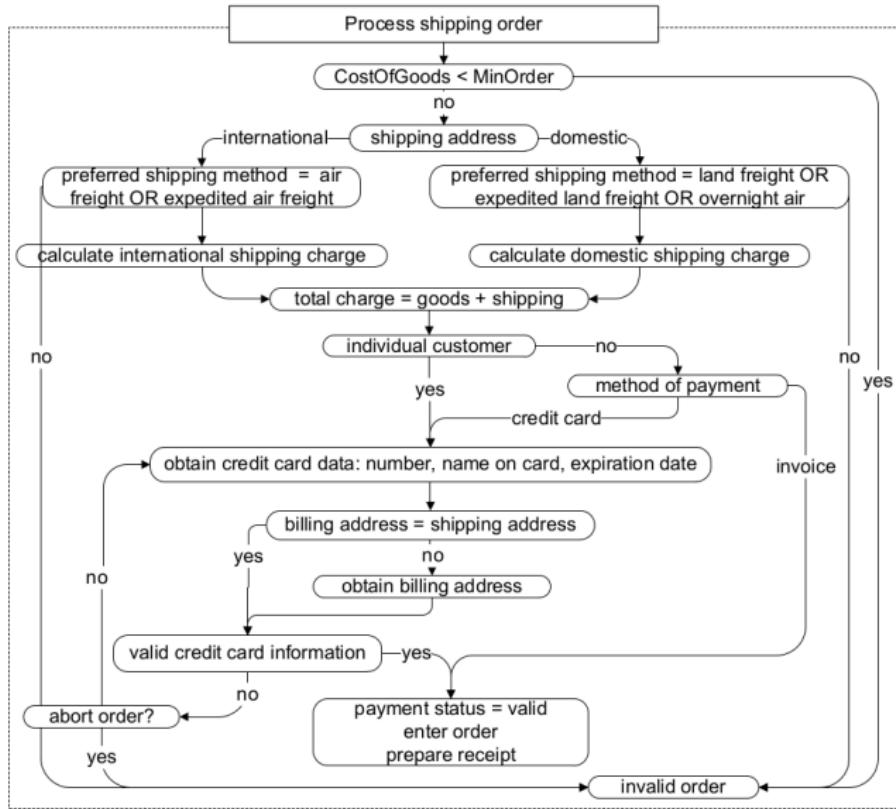
# Derive Test Cases from Control Flow Graphs

- There is a very simple way: inputs are linked to branches
- Thus, test case specification will be of the form:
  - “make this condition be true/false”
  - “make this enumeration be equal to this value”
- As usual, choose actual values to “realize” such test cases will not be easy
  - very program-dependent
- However, it could account for executions which could be missed by functional or structural testing



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# Example



# Example

## T-node

Case	Too small	Ship where	Ship method	Cust type	Pay method	Same addr	CC valid
TC-1	No	Int	Air	Bus	CC	No	Yes
TC-2	No	Dom	Air	Ind	CC	–	No (abort)

### Abbreviations:

Too small

CostOfGoods < MinOrder ?

Ship where

Shipping address, Int = international, Dom = domestic

Ship how

Air = air freight, Land = land freight

Cust type

Bus = business, Edu = educational, Ind = individual

Pay method

CC = credit card, Inv = invoice

Same addr

Billing address = shipping address ?

CC Valid

Credit card information passes validity check?



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## Example

### T-branch

Case	Too small	Ship where	Ship method	Cust type	Pay method	Same addr	CC valid
TC-1	No	Int	Air	Bus	CC	No	Yes
TC-2	No	Dom	Land	—	—	—	—
TC-3	Yes	—	—	—	—	—	—
TC-4	No	Dom	Air	—	—	—	—
TC-5	No	Int	Land	—	—	—	—
TC-6	No	—	—	Edu	Inv	—	—
TC-7	No	—	—	—	CC	Yes	—
TC-8	No	—	—	—	CC	—	No (abort)
TC-9	No	—	—	—	CC	—	No (no abort)

## Abbreviations:

Too small      CostOfGoods < MinOrder ?

Ship where **Shipping address. Int = international. Dom = domestic**

Ship how Air = air freight, Land = land freight

Bus = business, Edu = educational, Ind = individual

CC = credit card, Inv = invoice

Pay method: CC = credit card, INV = invoice  
Same addr: Billing address = shipping address ?

Same add'l Billing address = shipping address? Credit card information passes validity check?

# Testing for Objected-Oriented Software

- Of course, white-box testing...
  - however, for some of the following techniques a class or an object file could be sufficient
- Conceptually, same as procedural software
  - 1 generate functional tests from specification
  - 2 add selected structural test cases
  - 3 work from unit testing (typically, single classes...) and small-scale integration testing toward larger integration
  - 4 system testing
- However, some techniques are tailored for OO software, to tackle OO software peculiarities
  - short methods (e.g., getters and setters)
  - sequences of same-class methods calls are important
  - polymorphism, dynamic binding, generics, **overloading**...



# Object-Oriented Software Characteristics

## *State-dependent behaviour*

- values for attributes of classes are important
- inputs of methods do not tell the full story
- often, methods may have no inputs at all!
- e.g., the `is_right` method of the `Triangle` class does not have inputs
- but the result depends on the current values of the attributes
- thus, testing for `is_right` does require generating input values, even if it does not have any input



# Object-Oriented Software Characteristics

## *Encapsulation*

- suppose a `scale` method is present in class `Triangle`: how to check if the result is ok?
- as another example, suppose the `Triangle` class had coordinates of points (as `private`)
- suppose a `rotate` method is present
- using some external class for testing, how to check the result of `rotate`, given that attributes are `private`?



# Objected-Oriented Software Characteristics

- How to cope with these former problems?
- Solution 1: modify the code
  - add friend functions (only C++, not available in Java)
  - add getter and/or setter methods
  - make (some) members public
  - should be avoided, unless such modifications are kept in production
  - tested and released code should be the same
- Solution 2: consider sequences of calls
  - very program-dependent
  - if not possible, then there is some error for sure...



# Objected-Oriented Software Characteristics

## *Inheritance*

- here the problem is: supposing I tested the super class, should I test all methods in the subclass?
- new methods: of course, test is required
- overridden inherited methods: same as new methods
  - however, may call ancestor in some cases, for which re-test could be avoided
- non-overridden inherited methods:
  - most does not require re-test
  - however, in some cases re-test is needed
  - e.g., for side effects: a protected member of the super class may be used in the method, and be modified by the subclass...
  - may entail generating new test cases

# Object-Oriented Software Characteristics

## Polymorphism

```
class Animal {  
    public void animalSound() {  
        System.out.println("The animal makes a sound");  
    }  
}  
  
class Pig extends Animal {  
    public void animalSound() {  
        System.out.println("The pig says: wee wee");  
    }  
}  
  
class Dog extends Animal {  
    public void animalSound() {  
        System.out.println("The dog says: bow wow");  
    }  
}  
  
class Main {  
    public static void main(String[] args) {  
        Animal myAnimal = new Animal(); // Create a Animal object  
        Animal myPig = new Pig(); // Create a Pig object  
        Animal myDog = new Dog(); // Create a Dog object  
        myAnimal.animalSound();  
        myPig.animalSound();  
        myDog.animalSound();  
    }  
}
```

# Object-Oriented Software Characteristics

## *Polymorphism and dynamic binding*

- polymorphism: seems to call superclass methods, but subclass methods are invoked
- dynamic binding: again, which function is called is not known at compilation time
  - Java: using reflection or lambdas
  - C++: using pointers (and lambdas)
- need to test the same method on different class instances
- actually same as for inherited overridden methods, but invocation is different



# Objected-Oriented Software Characteristics

**Abstract classes** may need to be tested

- cannot be instantiated: only (non-abstract) subclasses may
- thus, contexts might be created for testing purposes only

**Overload** functions with same name but different arguments

- consider all possibilities

**Generics/Templates** functions and classes where arguments/return types are parameters

- consider all possibilities, given testing budget

**Exception handling** additional (exceptional) control flow

- design test cases to raise exceptions

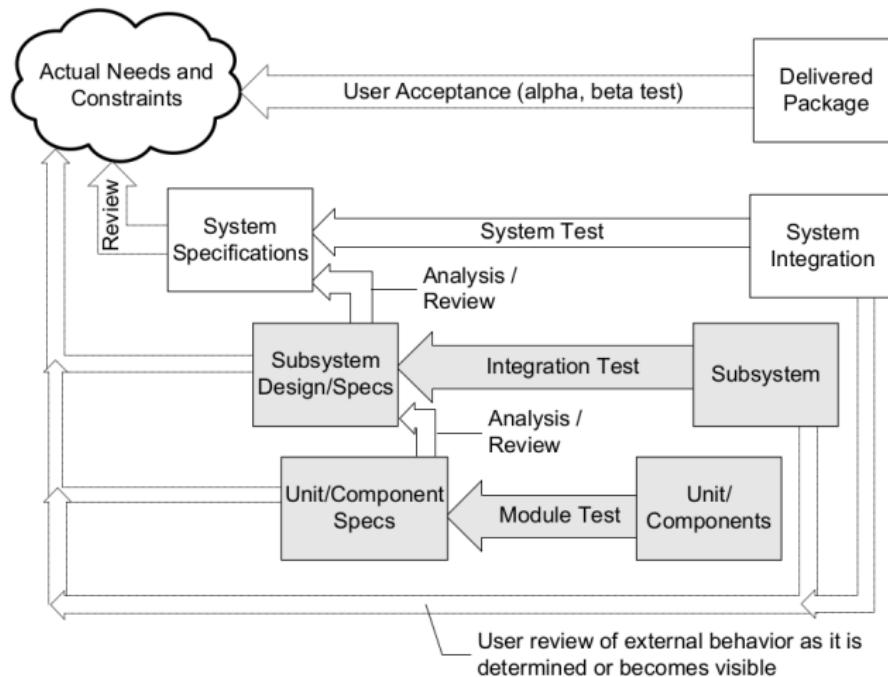


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# Impact of Objected Oriented Tailored Techniques



A&T Activities that require specific approaches for OO SW

# Objected-Oriented Software Testing

Mainly 3 stages, from single class to system integration

- intraclass: testing each class in isolation
  - also called unit testing
- interclass: testing class integration
  - also called integration testing
- system and acceptance: independent of design



# Objected-Oriented Software Testing Stages: Intraclass

Repeat the following for each class:

- if it is abstract, derive a set of instantiations
  - if not available, do this for testing only
- for each method in the class, determine whether to test it or not
  - including constructors and inherited methods
  - do not consider polymorphism or dynamic binding here
  - inheritance allows re-use of test cases
  - inheritance allows to skip testing of some methods
  - inheritance allows to skip testing of some inputs of some methods
- for the more complex methods in the class, design tests as for procedural software
  - may entail considering some members as further inputs

# Objected-Oriented Software Testing Stages: Intraclass

Repeat the following for each class (continued):

- derive test cases basing on a state machine model of the class behaviour, if available
  - that is: consider sequence of calls to the class methods
  - state and transition coverage for testing
  - kind of black-box (functional) testing inside white-box testing
- generate additional test cases considering structural testing techniques
  - again for sequences of calls
  - methods may be added/removed in implementation w.r.t. specification
- derive test cases for exception handling
  - both exceptions which are only thrown and exceptions which are caught and handled
- derive test cases for polymorphic methods and for generics
  - as for abstract classes: may require to instantiate a superclass for testing purposes only



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# Techniques for Inheritance

- Inheritance cannot introduce errors per se
  - though it is the base for polymorphism
- However, it can be exploited to understand when tests can be reused
- To this aim, distinguish methods of a subclass in:
  - new: not present in the superclass
    - present = same name & same parameters (implies same return)
    - recursive: present in the superclass and left unchanged
    - redefined: present in the superclass and body changed
- Also distinguish if the method was abstract in the superclass
  - abstract new, recursive, redefined



# Techniques for Inheritance

- To start with, you always begin testing from the superclass
  - if a hierarchy is present, go to the higher superclass
  - class diagram is needed
- Thus, recursive methods need not to be retested
  - abstract recursive only tested with stubs, as an implementation is lacking
- (Abstract) redefined and new methods always need to be retested
  - for non-abstract redefined, it may be possible to skip some inputs
- To keep track of what to retest, a *testing history table* may be used
- When a new subclass is considered, the table is scanned to understand which methods needs retesting

# Testing History Tables

- Testing history tables are organized as follows:
  - rows are methods
  - columns are of 4 types:
    - intraclass functional
    - intraclass structural (not for abstract)
    - interclass functional (not for local)
    - interclass structural (not for local or abstract)
  - “local” methods are those which only call other methods of the same class
  - entries are the corresponding test set, plus a flag
    - executable/not executable



# Testing History Table Example

```
1  /** One line item of a customer order (abstract). */
2  public abstract class LineItem {
3
4      /** The order this LineItem belongs to. */
5      protected Order order;
6
7      /** Constructor links item to owning order. Must call in subclasses. */
8      public LineItem(Order _order) { order = _order; }
9
10     /** Stock-keeping unit (sku) is unique key to all product databases. */
11     public String sku;
12
13     /** Number of identical units to be purchased. */
14     public int units=1;
15
16     /** Has this line item passed all validation tests? */
17     public abstract boolean validItem();
18
19     /** Price of a single item. */
20     public abstract int getUnitPrice(AccountType accountType);
21
22     /** Extended price for number of units */
23     public int getExtendedPrice(AccountType accountType)
24     { return units * this.getUnitPrice(accountType); }
25
26     // Dimensions for packing and shipping (required of all top-level items)
27     /** Weight in grams */
28     public abstract int getWeightGm();
29     /** Height in centimeters */
30     public abstract int getHeightCm();
31     /** Width in Centimeters. */
32     public abstract int getWidthCm();
33     /** Depth in Centimeters */
34     public abstract int getDepthCm();
35 }
```



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# Testing History Table Example

Method	Intra funct	Intra struct	Inter funct	Inter struct
LineItem	$\langle TS_{LI1}, Y \rangle$	$\langle TS_{LI2}, Y \rangle$	$\langle TS_{LI3}, Y \rangle$	$\langle TS_{LI4}, Y \rangle$
validItem	$\langle TS_{vI1}, N \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$
getUnitPrice	$\langle TS_{gUP1}, N \rangle$	$\langle -, - \rangle$	$\langle TS_{gUP3}, N \rangle$	$\langle -, - \rangle$
getExtendedPrice	$\langle TS_{gXP1}, Y \rangle$	$\langle TS_{gXP2}, Y \rangle$	$\langle TS_{gXP3}, Y \rangle$	$\langle TS_{gXP4}, Y \rangle$
getWeightGm	$\langle TS_{gWG1}, N \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$
getHeightCm	$\langle TS_{gHC1}, N \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$
getWidthCm	$\langle TS_{gWC1}, N \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$
getDepthCm	$\langle TS_{gDC1}, N \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$

**Legend:**  $\langle TS_I, B \rangle$  refers to test set  $I$ , to be executed if  $B = Y$ .

$\langle -, - \rangle$  means no applicable tests.

Of course, to test the two with  $Y$  a subclass is needed, possibly only for testing purposes



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7      /** Constructor links item to owning order. Must call in subclasses. */
8      public LineItem(Order _order) { order = _order; }
9
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24     { return units * this.getUnitPrice(accountType); }
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30     public abstract int getHeightCm();
31     /** Width in Centimeters. */
32     public abstract int getWidthCm();
33     /** Depth in Centimeters */
34     public abstract int getDepthCm();
35 }
```



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# Testing History Table Example

```
public abstract class CompositeItem extends LineItem {  
  
    /**  
     * A composite item has some unifying name and base price  
     * (which might be zero) and has zero or more additional parts,  
     * which are themselves line items.  
     */  
    private Vector parts = new Vector();  
  
    /**  
     * Constructor from LineItem, links to an encompassing Order.  
     */  
    public CompositeItem(Order _order) {  
        super(_order);  
    }  
  
    public int getUnitPrice(AccountType accountType) {  
        Pricelist prices = new Pricelist();  
        int price = prices.getPrice(sku, accountType);  
        for (Enumeration e = parts.elements(); e.hasMoreElements(); )  
        {  
            LineItem i = (LineItem) e.nextElement();  
            price += i.getUnitPrice(accountType);  
        }  
        return price;  
    }  
}
```



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# Testing History Table Example

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getUnitPrice	$\langle TS_{gUP1}, N \rangle$	$\langle -, - \rangle$	$\langle TS_{gUP3}, N \rangle$	$\langle -, - \rangle$
getExtendedPrice	$\langle TS_{gXP1}, Y \rangle$	$\langle TS_{gXP2}, Y \rangle$	$\langle TS_{gXP3}, Y \rangle$	$\langle TS_{gXP4}, Y \rangle$
getWeightGm	$\langle TS_{gWG1}, N \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$
getHeightCm	$\langle TS_{gHC1}, N \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$
getWidthCm	$\langle TS_{gWC1}, N \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$
getDepthCm	$\langle TS_{gDC1}, N \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$

**Legend:**  $\langle TS_I, B \rangle$  refers to test set  $I$ , to be executed if  $B = Y$ .

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validItem	$\langle TS_{vI1}, N \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$
getUnitPrice	$\langle TS_{gUP1}, Y \rangle$	$\langle TS'_{gUP2}, Y \rangle$	$\langle TS_{gUP3}, Y \rangle$	$\langle TS'_{gUP4}, Y \rangle$
getExtendedPrice	$\langle TS_{gXP1}, N \rangle$	$\langle TS_{gXP2}, N \rangle$	$\langle TS_{gXP3}, N \rangle$	$\langle TS_{gXP4}, N \rangle$
getWeightGm	$\langle TS_{gWG1}, N \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$
getHeightCm	$\langle TS_{gHC1}, N \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$
getWidthCm	$\langle TS_{gWC1}, N \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$
getDepthCm	$\langle TS_{gDC1}, N \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$	$\langle -, - \rangle$
CompositeItem	$\langle TS'_{CM1}, Y \rangle$	$\langle TS'_{CM2}, Y \rangle$	$\langle TS'_{CM3}, Y \rangle$	$\langle TS'_{CM4}, Y \rangle$



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# Objected-Oriented Software Testing Stages: Intraclass

Repeat the following for each class:

- if it is abstract, derive a set of instantiations
  - if not available, do this for testing only
- for each method in the class, determine whether to test it or not
  - including constructors and inherited methods
  - do not consider polymorphism or dynamic binding here
  - inheritance allows re-use of test cases
  - inheritance allows to skip testing of some methods
  - inheritance allows to skip testing of some inputs of some methods
- for the more complex methods in the class, design tests as for procedural software
  - may entail considering some members as further inputs

# Objected-Oriented Software Testing Stages: Intraclass

Repeat the following for each class (continued):

- derive test cases basing on a state machine model of the class behaviour, if available
  - that is: consider sequence of calls to the class methods
  - state and transition coverage for testing
  - kind of black-box (functional) testing inside white-box testing
- generate additional test cases considering structural testing techniques
  - again for sequences of calls
  - methods may be added/removed in implementation w.r.t. specification
- derive test cases for exception handling
  - both exceptions which are only thrown and exceptions which are caught and handled
- derive test cases for polymorphic methods and for generics
  - as for abstract classes: may require to instantiate a superclass for testing purposes only



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# Intraclass Testing: State Machines

Two cases:

- no state machine in specification, thus draw one from informal specifications
  - done for testing only, may need remapping for method names
- state machine diagram present in specification
  - typically a UML statechart, may be more complicated because of:
    - superstates: to be replaced with a flattening
    - considering all ingoing and outgoing transitions...
- in both cases, transitions in state machine diagram are usually labeled with class methods
  - thus, we obtain test cases based on *sequences* of calls
  - some sense, it is more than unit testing...



# State Machines from Informal Specifications

## From Informal Specs to Transition Coverage

### An Informal Specification of Class *Slot*

**Slot** represents a configuration choice in all instances of a particular model of computer. It may or may not be implemented as a physical slot on a bus. A given model may have zero or more slots, each of which is marked as required or optional. If a slot is marked as "required," it must be bound to a suitable component in all legal configurations.

Class Slot offers the following services:

**Incorporate:** Make a slot part of a model, and mark it as either required or optional. All instances of a model incorporate the same slots.

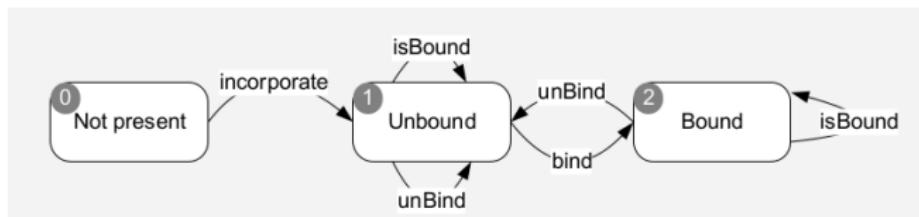
*Example:* We can incorporate a required primary battery slot and an optional secondary battery slot on the Chipmunk C20 laptop that includes two battery slots. The C20 laptop may then be sold with one battery or two batteries, but it is not sold without at least the primary battery.

**Bind:** Associate a compatible component with a slot. *Example:* We can bind slot primary battery to a Blt4, Blt6, or Blt8 lithium battery or to a Bcdm4 nickel cadmium battery. We cannot bind a disk drive to the battery slot.

**Unbind:** The unbind operation breaks the binding of a component to a slot, reversing the effect of a previous bind operation.

**IsBound:** Returns true if a component is currently bound to a slot, or false if the slot is currently empty.

# State Machines from Informal Specifications

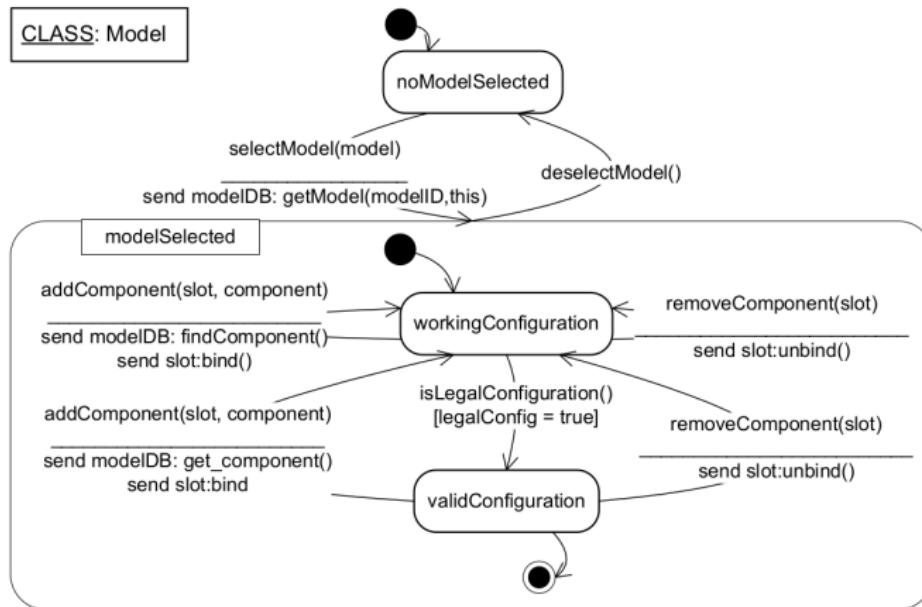


TC-1: incorporate, isBound, bind, isBound

TC-2: incorporate, unBind, bind, unBind, isBound

Transition coverage = 100%

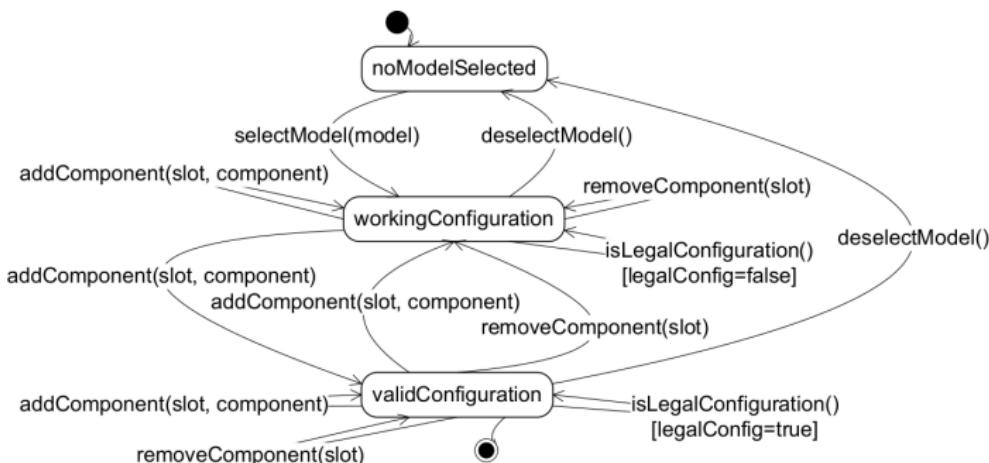
# State Machines in Specifications



addComponent etc are self-loops



# State Machines in Specifications



Actions omitted for brevity  
Two `deselectModel`, one `selectModel`

# State Machines in Specifications

## Test Case $TC_A$

```
selectModel(M1)  
addComponent(S1,C1)  
addComponent(S2,C2)  
isLegalConfiguration()
```

## Test Case $TC_B$

```
selectModel(M1)  
deselectModel()  
selectModel(M2)  
addComponent(S1,C1)  
addComponent(S2,C2)  
removeComponent(S1)  
isLegalConfiguration()
```

## Test Case $TC_C$

```
selectModel(M1)  
addComponent(S1,C1)  
removeComponent(S1)  
addComponent(S1,C2)  
isLegalConfiguration()
```

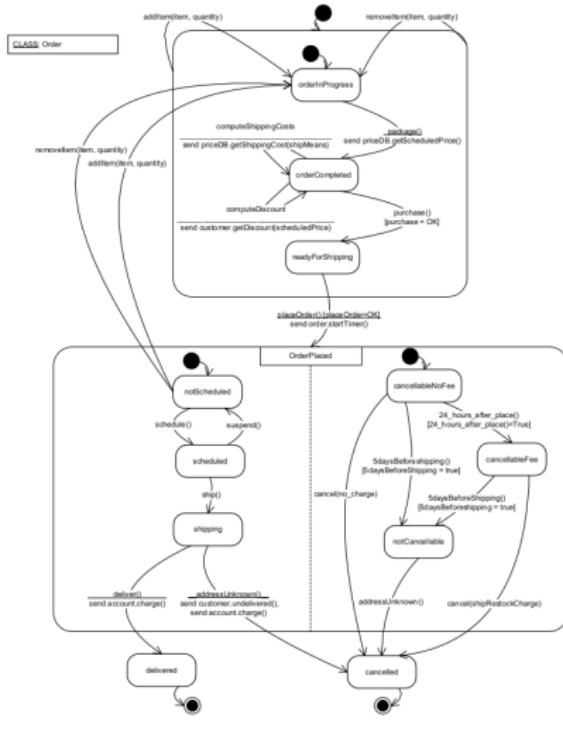
## Test Case $TC_D$

```
selectModel(M1)  
addComponent(S1,C1)  
addComponent(S2,C2)  
addComponent(S3,C3)  
deselectModel()  
selectModel(M1)  
addComponent(S1,C1)  
isLegalConfiguration()
```

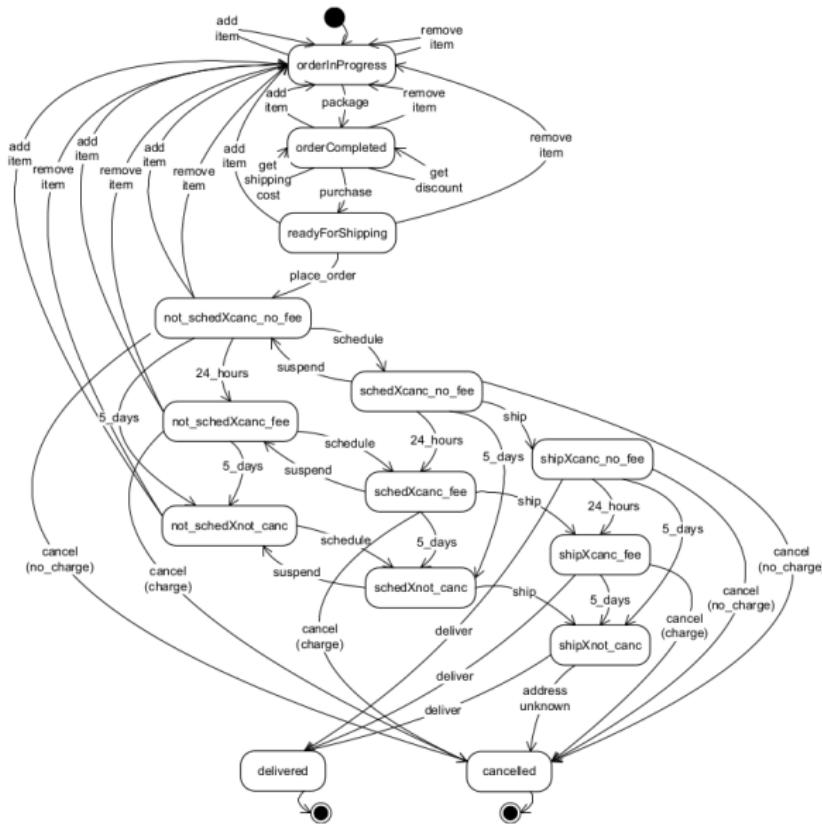
## Test Case $TC_E$

```
selectModel(M1)  
addComponent(S1,C1)  
addComponent(S2,C2)  
addComponent(S3,C3)  
removeComponent(S2)  
addComponent(S2,C4)  
isLegalConfiguration()
```

# State Machines in Specifications



# State Machines in Specifications



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# State Machines in Specifications

Test Case $TC_A$	Test Case $TC_B$	Test Case $TC_C$
<code>add_item() add_item() add_item() package() get_shipping_cost() get_discount() purchase() place_order() 24.hours() 5.days() schedule() ship() deliver()</code>	<code>add_item() add_item() <b>remove_item()</b> add_item() package() get_shipping_cost() get_discount() purchase() place_order() 24.hours() 24.hours() 5.days() schedule() ship() deliver()</code>	<code>add_item() add_item() 24.hours() add_item() package() get_shipping_cost() get_discount() purchase() place_order() <b>add_item()</b> package() get_shipping_cost() get_discount() purchase() place_order()</code>

Test Case $TC_D$	Test Case $TC_E$	Test Case $TC_F$
<code>add_item() add_item() package() get_shipping_cost() get_discount() purchase() place_order() <b>remove_item()</b> add_item() package() get_shipping_cost() get_discount()</code>	<code>purchase() place_order() 24.hours() schedule() ship() deliver()</code>	<code>add_item() add_item() package() get_shipping_cost() get_discount() purchase() place_order() schedule() <b>suspend()</b> 5.days() schedule() ship() deliver()</code>

Test Case $TC_G$	Test Case $TC_H$	Test Case $TC_I$
<code>add_item() add_item() package() get_shipping_cost() get_discount() purchase() place_order() schedule() ship() address.unknown()</code>	<code>add_item() add_item() package() get_shipping_cost() get_discount() purchase() place_order() schedule() 5.days() address.unknown()</code>	<code>add_item() add_item() package() get_shipping_cost() get_discount() purchase() place_order() schedule() 24.hours() cancel()</code>



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# Objected-Oriented Software Testing Stages: Intraclass

Repeat the following for each class:

- if it is abstract, derive a set of instantiations
  - if not available, do this for testing only
- for each method in the class, determine whether to test it or not
  - including constructors and inherited methods
  - do not consider polymorphism or dynamic binding here
  - inheritance allows re-use of test cases
  - inheritance allows to skip testing of some methods
  - inheritance allows to skip testing of some inputs of some methods
- for the more complex methods in the class, design tests as for procedural software
  - may entail considering some members as further inputs

# Objected-Oriented Software Testing Stages: Intraclass

Repeat the following for each class (continued):

- derive test cases basing on a state machine model of the class behaviour, if available
  - that is: consider sequence of calls to the class methods
  - state and transition coverage for testing
  - kind of black-box (functional) testing inside white-box testing
- generate additional test cases considering structural testing techniques
  - again for sequences of calls
  - methods may be added/removed in implementation w.r.t. specification
- derive test cases for exception handling
  - both exceptions which are only thrown and exceptions which are caught and handled
- derive test cases for polymorphic methods and for generics
  - as for abstract classes: may require to instantiate a superclass for testing purposes only



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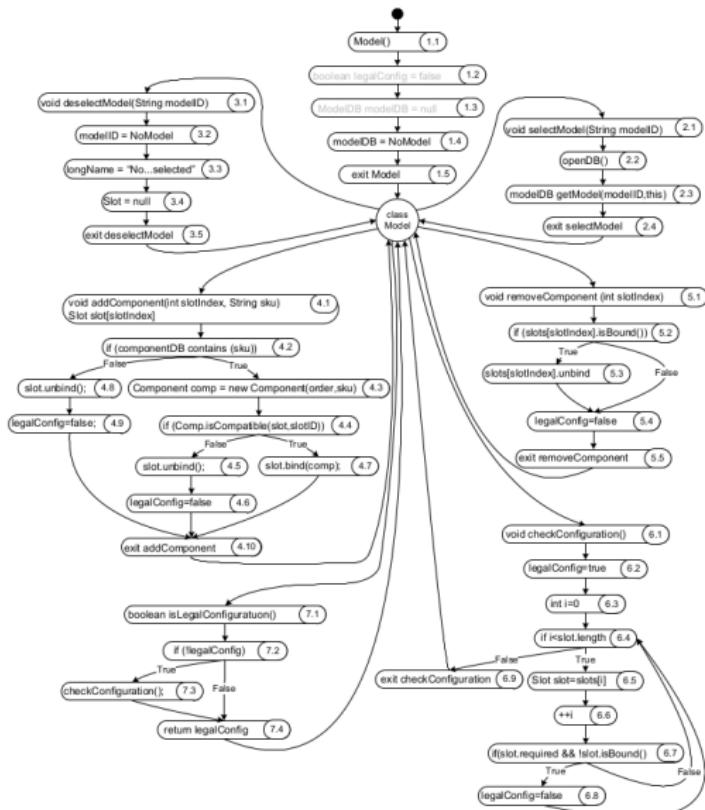
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# Structural Intraclass Testing

- Integrate “black-box” testing: did we miss something?
- *Intraclass CFG*
  - CFGs for each method, connected by calls
- For each add member value, consider all DU pairs in the intraclass CFG
- New test cases are of the form:
  - start with a constructor
  - pass through the definition
  - end with the use without going through any other definition
- All DU pairs adequacy criterion is typically used



# Intraclass CFG: Example



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# Objected-Oriented Software Testing Stages: Intraclass

- Derive test cases basing on a state machine model of the class behaviour, if available
  - that is: consider sequence of calls to the class methods
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  - kind of black-box (functional) testing inside white-box testing
- Generate additional test cases considering structural testing techniques
  - again for sequences of calls
  - methods may be added/removed in implementation w.r.t. specification
- Derive test cases for exception handling
  - both exceptions which are only thrown and exceptions which are caught and handled
- Derive test cases for polymorphic methods and for generics
  - instantiate a superclass in all possible ways

# Techniques for Exceptions

- Exceptions are by themselves an help to testing
  - in procedural programming, overlooking error codes returned by functions often occurs
  - exceptions handling mitigates this problem, as an exception is certain to interrupt normal control flow
  - cost: implicit control flows are added
- Building a CFG with exceptions is impracticable
  - also complicated by the fact that exception binding for handlers is dynamic



# Techniques for Exceptions

Techniques by Exception type:

- Program errors (bad subscript or casts etc)
  - can usually be discarded: we are already looking for them in the previous steps
  - if a custom handler is present, test it by creating a class which forces the given error (*stub*)
- Abnormal cases (memory exhausted, file not present etc)
  - raise them and check the handler if present
  - again, a stub might be necessary
- Exception propagation
  - A calls B which raises E, but A does not handle E
  - E will go up in the calls stack, till when a handler is found (if not, the application is closed, which is bad)
  - check at least some of such exception chains



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# Techniques for Polymorphism and Dynamic Binding

- If the possible morphs or binding are just a few, simply consider them all
- However, in some cases there may be many combinations
  - cases explosion, cannot be considered exhaustively
- You may need to *imagine* possible instations if you are testing a library rather than a complete program
- A variation of Pairwise Testing may be used!



# Object-Oriented Software Characteristics

```
class Animal {  
    public void animalSound() {  
        System.out.println("The animal makes a sound");  
    }  
}  
  
class Pig extends Animal {  
    public void animalSound() {  
        System.out.println("The pig says: wee wee");  
    }  
}  
  
class Dog extends Animal {  
    public void animalSound() {  
        System.out.println("The dog says: bow wow");  
    }  
}  
  
class Main {  
    public static void main(String[] args) {  
        Animal myAnimal = new Animal(); // Create a Animal object  
        Animal myPig = new Pig(); // Create a Pig object  
        Animal myDog = new Dog(); // Create a Dog object  
        myAnimal.animalSound();  
        myPig.animalSound();  
        myDog.animalSound();  
    }  
}
```

# Example

3 points of choice:

- instantiation of Credit
- instantiation of Account
- instantiation of CreditCard

```
abstract class Credit {  
    ...  
    abstract boolean validateCredit( Account a, int amt, CreditCard c);  
    ...  
}
```



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# Example

15 vs 45 (exhaustive)

Account	Credit	creditCard
USAccount	EduCredit	VISACard
USAccount	BizCredit	AmExpCard
USAccount	individualCredit	ChipmunkCard
UKAccount	EduCredit	AmExpCard
UKAccount	BizCredit	VISACard
UKAccount	individualCredit	ChipmunkCard
EUAccount	EduCredit	ChipmunkCard
EUAccount	BizCredit	AmExpCard
EUAccount	individualCredit	VISACard
JPAccount	EduCredit	VISACard
JPAccount	BizCredit	ChipmunkCard
JPAccount	individualCredit	AmExpCard
OtherAccount	EduCredit	ChipmunkCard
OtherAccount	BizCredit	VISACard
OtherAccount	individualCredit	AmExpCard



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# Techniques for Parameterized Types

- “Generics” in Java, “templates” in C++
  - typical example: an array where the type of each entry may be decided when instantiating the object
- Only class instantiations can be tested
  - as for abstract methods
  - cannot know in advance which type will be used
  - thus, some reasonable forecast should be used
  - use Pairwise Testing if the parametric types are more than one
- Testing may be split in two parts:
  - showing that some instantiation is correct
  - showing that all permitted instantiations behave “identically”



# Objected-Oriented Software Testing Stages: Interclass

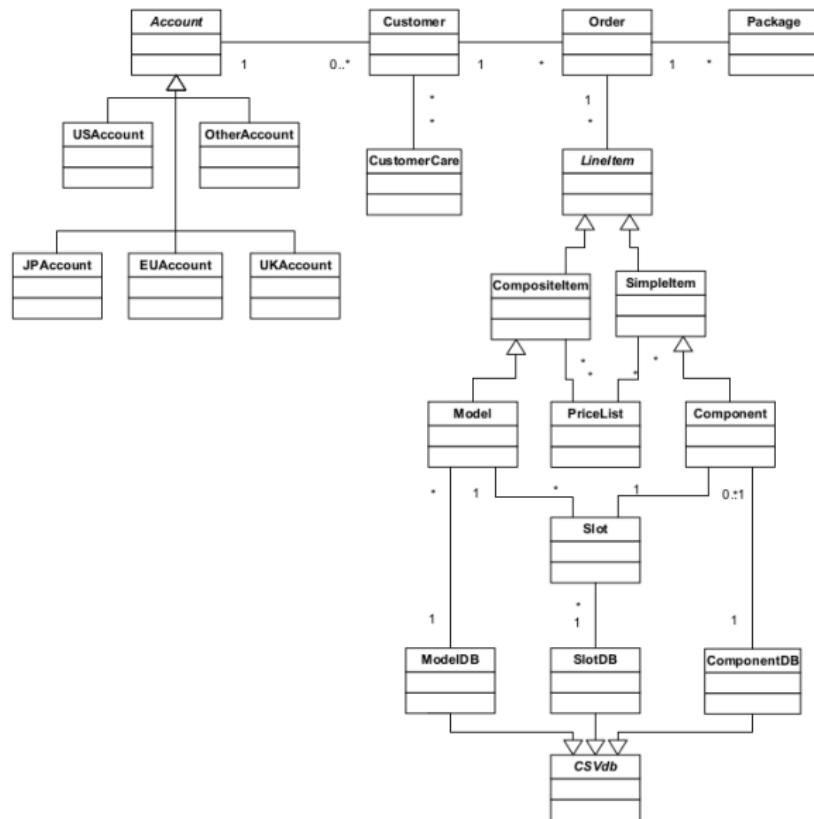
- Identify which classes should be tested together (*cluster*)
  - typically, because they call each other methods
  - either statically (on the class) or dynamically (on classes instances)
- The previous step is to be performed *incrementally*:
  - first consider pairs of classes, then triplets, etc
  - in some cases, there could be some minimum subset of classes to be considered
  - we may say that OO helps in identifying units for unit and integration testing...
- Functional test for the given cluster
  - also considering data flow between calls
- Integrate the previous intraclass exception handling test cases with interclass exception handling test cases
- Same for the polymorphism

# Interclass Testing

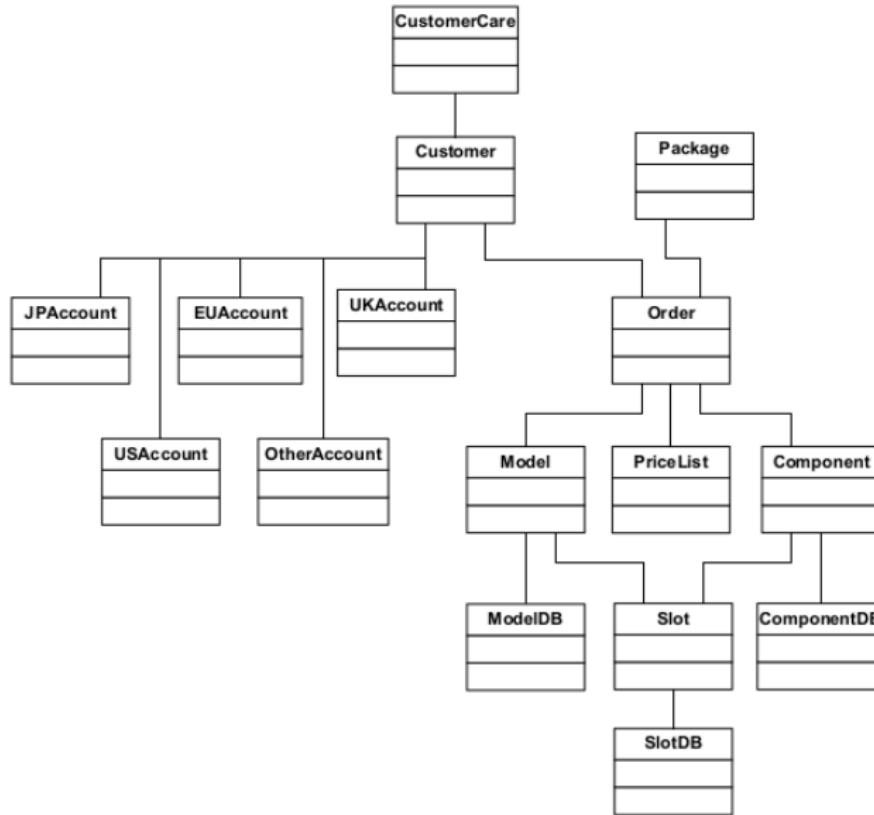
- Two main workhorses: use/include relation and sequence/collaboration diagrams
- Use/include is very simple to derive from UML Class Diagrams
  - typically drawn with simple vertical lines: the class on the top depends on the one on the bottom
  - either because of usage (aggregation) or inclusion (inheritance)
  - abstract classes not included
- Once you have it, start testing from the bottom
  - difficult to generalize, experience helps
  - need to select a subset of interactions among the possible combinations of method calls and class states



# From UML...



# ... to Use/Include Diagram

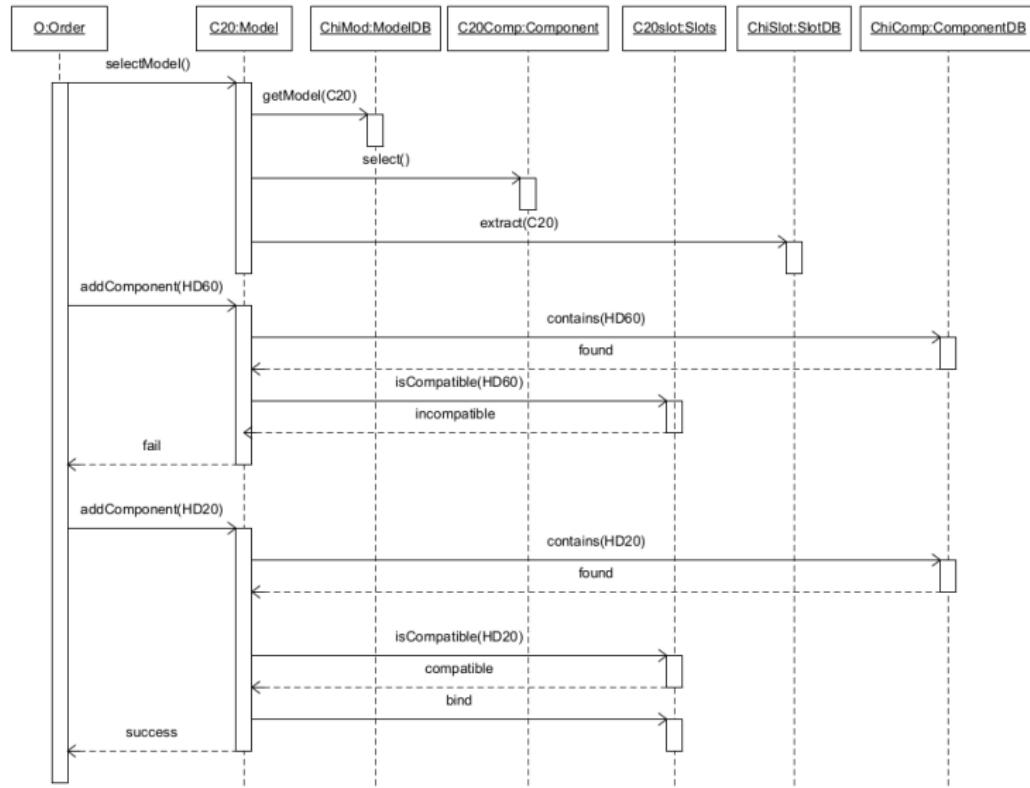


# Interclass Functional Testing

- Sequence diagrams may be used to design test which cover all possible exchanges
- Furthermore, some interaction in the sequence diagram may be replaced by another, to check if errors are handled correctly
- State diagrams should cover all possible “relevant” behaviours
  - of course, if we have a state diagram involving multiple classes, that could be used for interclass testing in the very same way as in intraclass testing
- Instead, sequence diagrams are a selection made by designers
- Thus, they are very valuable for testing



# Example



# Interclass Structural Testing

- Classification of methods as:
  - inspectors: only read the class state
  - modifiers: only write the class state
  - inspectors/modifiers: both
  - getters are inspectors, setters are modifiers
  - “class state”: at least one variable in the class state
- By going bottom-up in the whole class dependencies:
  - invocations of modifier methods and inspector/modifiers of leaf classes are considered as definitions
  - invocations of inspectors and inspector/modifiers in other classes are treated as uses
- Proceed as in definition-use pairs



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# From Test Case Specifications to Test Cases

- That is: we want the raw inputs
- Keeping specification and generation separate aids in reducing impact of small changes in the software development
- Some test case specifications are relatively simple to be completed
  - e.g., those coming from partition/category method
  - sometimes, they are already with raw inputs
- Others may require some other effort
  - e.g. “a sorted sequence, length greater than 2, with items in ascending order with no duplicates”
- Two or more test cases specifications may be dependent on each other



# From Test Case Specifications to Test Cases

- Some test case specifications may require an actual computation to be translated into test cases
  - e.g., “traverse these transitions in this program state machine”  
→ find the data which cause that transitions
  - model checking may be used!
  - say the transitions are impossible and collect the counterexample...



# Tools Which Generate Test Cases

- Though it is undecidable, some tools are actually able to output test cases for code
  - typically, for C code
  - typically, incomplete tools, but better than nothing
- CBMC: given a C code, generates test cases for some types of coverage
  - especially MC/DC
  - free, for any platform
- Reactis: given a C code, generates test cases for all types of coverage
  - commercial, for Windows
- Unit testing only, with some support for call coverage



# Tests Execution

- Executing tests is not always straightforward
- General goal: once we have test cases, we should perform the last steps as automatically as possible
  - not always possible or practical, e.g., if we want to check a GUI...
- Mastering the following techniques is important:
  - creating scaffolding for test execution
  - (automatically) distinguishing between correct and incorrect results
  - run-time support for generating and managing test data
    - e.g., a database storing information about each test case



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# Scaffolding

- Literally, the temporary structures erected around a building during construction or maintenance
- Practically, it is any software which is developed to test some other software
  - a software for scaffolding of Java programs is, e.g., JUnit
  - similar tools exist for other languages, e.g., phpUnit
  - for more complex testing, developing a dedicated software may be needed
  - could require an high cost, up to half of the code developed for the entire project
- Deciding to create a new software for scaffolding or not depends on budget



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# Scaffolding

- Scaffolding may be divided into:

- drivers for calling programs

- stubs for functions called by the program

- oracles to check results

- program instrumentation adding statements for monitoring/measuring

- test support create a database to record info like:

- test suites for different program releases
    - how many times (across different program releases) a test case has been executed and with which result
    - test suite creators
    - ...

- test harnesses for the overall testing environment

# Scaffolding Techniques: Stubs

- We want to test from early stages: very few components will be available
  - may be avoided if design takes testing into consideration, so components are implemented in an order which enables testing
  - cannot be done in all cases
- Stubs replace (unavailable) portions of the program to be tested
- Easiest form of stub: *mock*
  - replace a function with another function taking the same parameters and outputting a fixed value
  - “output” in a broad sense: also print a string or set global variables
  - in some cases, mock can be generated automatically from source code

# Scaffolding Techniques: Drivers

- For many cases, input for some ITF is provided from the beginning
  - as in the examples of the collapsing spaces and the roots of a second degree equation
- Then, we simply have to wait for the ITF to return its output
- Otherwise, the input must be provided with some given timing (e.g., for controllers)
- In both cases, a *driver* is needed to run the software with the given input
  - program-dependent, though automatable for unit testing (e.g., JUnit)
  - may be easy: instantiate a class and call some methods
  - may be difficult: create a pool of processes to handle inter-process communication in some integration or system testing



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# Scaffolding Techniques: Harnesses

- What about the cycle needed to take each test case  $T$  in the test suite  $S$  and run the driver on  $T$ ? We need *test harnesses*
  - sometimes, it may be written in such a case to take test case specifications
  - see the black-box examples
- They are responsible also for:
  - checking the result
    - we will be back on how to do this
  - any further input coming from the environment and not provided since the beginning
    - e.g., a controller for an airplane reads air speed every  $t$  milliseconds: the test harness must provide such info
    - e.g., a network traffic generator to check a Web application resilience
    - also part of test case specification



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# Test Oracles

- Again part of scaffolding (harness): how to check results of test cases?
  - human intervention to be avoided whenever possible: expensive and unreliable
  - unless we are testing usability of GUIs...
- A *test oracle* is something distinguishing correct from uncorrect test results
  - automated test oracles: it is a software
- Partial oracle: one with false positives
  - sometimes good because cost-effective, especially for early testing
- Oracle with false negatives: to be avoided
  - requires manual inspection to understand it is a true or false negative

# Test Oracles Techniques

- Comparison-based oracles
  - test cases are (input, output) pairs, so oracle simply check if result is equal to expected output
  - may be not bit-to-bit equal and still be ok
  - this is typically the case for test harness
- How to have correct (input, output) pairs?
  - could seem a self-referencing solution...
  - depends on the application and the problem
- Solution 1: create an output and produce a corresponding input
  - sorting: create a sorted list and permute it...
  - needs some adjustment w.r.t. Category-Partition and Catalog-based Testing
  - e.g.: for the collapsing spaces, first generate a single-spaced string, and then repeat some spaces...
  - e.g.: for the equation roots, generate at random  $r_1, r_2, a$  and then put  $b = a(r_1 + r_2)$ ,  $c = ar_1r_2$



# Test Oracles Techniques

- Solution 2: use some other software
  - may be already available, but not usable in production code
    - e.g., due to intellectual rights, or because it is too slow
  - may be written by test engineers
    - e.g., for the collapsing spaces, a (slower) function may be written by only looking at the specification
  - the important thing is that it is independent by the program to be tested
  - not necessarily better: it may be ok if both the program and the oracle fail rarely enough
    - or if it is much slower
  - in such a way, there is time to inspect both programs to see which is right whenever the output differs
  - but failures must be independent



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# Test Oracles Techniques: Capture and Replay

- Solution 3: use humans, but only once
- Especially ok for visual responses of graphical interfaces
- The human judges the output, and its evaluation is recorded together with the input
- Starting from that point, any other re-execution of the test remembers the human evaluation
- Not always simple or cost-effective: small differences in a graphical interface should be ok but may trigger a false negative



# Test Oracles Techniques

- Oracles need not to be comparison-based: we may implement some software able to check the output
  - using specifications, of course
  - often called *Property-based Testing*
- Checking if an output is correct is often easier than producing it
  - e.g., routing problem, but also the collapsing spaces and 2nd order equation roots computation we saw before...
- Special case of partial oracles: drop optimality
  - e.g., in optimal routing problem, we only check if the output route is correct, not if it is optimal
  - often combined with comparison-based oracle:
    - cheap, partial oracle for large test suite
    - heavy test suite with precomputed outputs for a subset of the suite

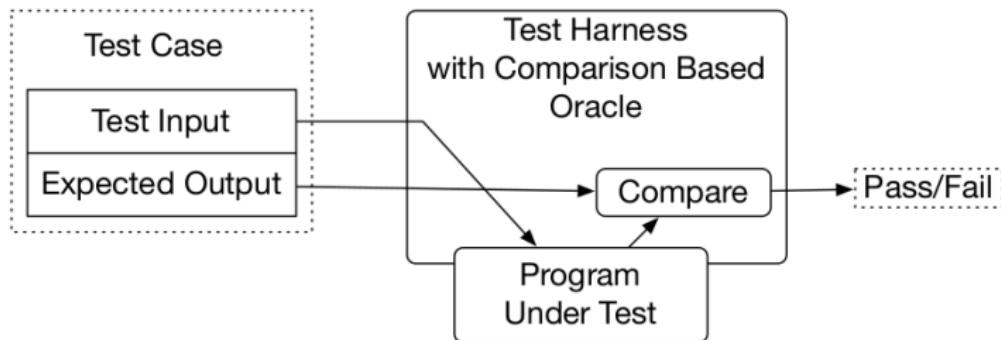


# Test Oracles Techniques

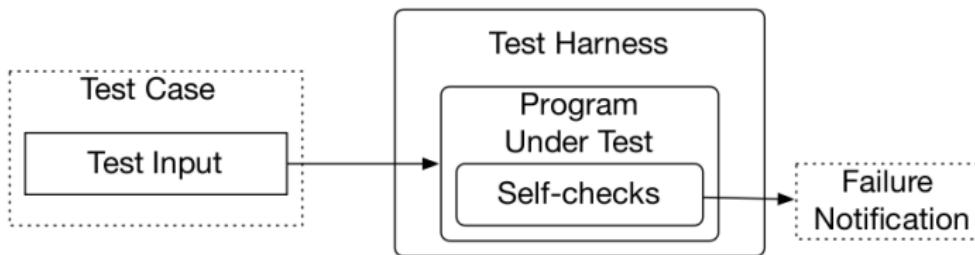
- Self-checks: assertions in the code
  - typically from the original designers, but could be added by testers
  - better an assertion failure than a BSOD
- Lightweight assertions may be left in production code
  - so, usable for testing
- Heavyweight assertions may be left in code and compiler directives can be used to optimize them out
  - use them in testing, then strip them out



# Scaffolding Techniques: Harnesses



# Scaffolding Techniques: Harnesses



# Scaffolding for OO Software

- Stubs only needed if we want to test a part of the program when some other related part is not ready
- Drivers actually launch the experiments
  - not different from procedural testing
- Oracles are more difficult than procedural testing due to encapsulation
- Technique one: allow oracle to read private members
  - or add getters and setters
  - not a good idea: tested and delivered software would be different!
  - exploit language features: friend classes in C++
  - or package visibility in Java (also putting oracles in the same package)



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# Oracles for OO Software

- Technique two: consider equivalence between objects
  - especially useful for arrays and similar
  - an array is similar to a linked list: important is that they have the same values...
  - the oracle uses the equivalent data structure, if the original one is not available because private
- One sequence of method invocations is equivalent to another if the two sequences lead to the same object state
- This does not necessarily mean that their concrete representation is bit-for-bit equal



# Oracles for OO Software

## Test Case $TC_E$

```
selectModel(M1)
addComponent(S1,C1)
addComponent(S2,C2)
isLegalConfiguration()
deselectModel()
selectModel(M2)
addComponent(S1,C1)
isLegalConfiguration()
```

## Scenario $TC_{E1}$

```
selectModel(M2)
addComponent(S1,C1)
isLegalConfiguration()
```

EQUIVALENT

## Scenario $TC_{E2}$

```
selectModel(M2)
addComponent(S1,C1)
addComponent(S2,C2)
isLegalConfiguration()
```

NON-EQUIVALENT



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# Besides Testing: Inspection

- Have a human inspect the code
  - of course, the code must be inspectable
  - something could be done also automatically, see, e.g., lint and purify
- Not too much, it is boring
  - two hours a day
  - valuable for juniors, they see production code
  - reinspection is as hard as the first one
- Organize the work, perform the work, speak with developers
- Perform the work: typically with checklists
- Pair programming in Agile method: inspection included in implementation phase



# Example

Java Checklist: Level 1 inspection (single-pass read-through, context independent)		
FEATURES (where to look and how to check): Item (what to check)		
<b>FILE HEADER:</b> Are the following items included and consistent?	yes	no
Author and current maintainer identity		
Cross-reference to design entity		
Overview of package structure, if the class is the principal entry point of a package		
<b>FILE FOOTER:</b> Does it include the following items?	yes	no
Revision log to minimum of 1 year or at least to most recent point release, whichever is longer		
<b>IMPORT SECTION:</b> Are the following requirements satisfied?	yes	no
Brief comment on each import with the exception of standard set: <code>java.io.*</code> , <code>java.util.*</code>		
Each imported package corresponds to a dependence in the design documentation		
<b>CLASS DECLARATION:</b> Are the following requirements satisfied?	yes	no
The visibility marker matches the design document		
The constructor is explicit (if the class is not <code>static</code> )		
The visibility of the class is consistent with the design document		
<b>CLASS DECLARATION JAVADOC:</b> Does the Javadoc header include:	yes	no
One sentence summary of class functionality		
Guaranteed invariants (for data structure classes)		
Usage instructions		
<b>CLASS:</b> Are names compliant with the following rules?	yes	no
Class or interface: CapitalizedWithEachInternal-WordCapitalized		
Special case: If class and interface have same base name, distinguish as <code>ClassNameIfc</code> and <code>ClassNameImpl</code>		
Exception: <code>ClassNameEndsWithException</code>		
Constants (final): <code>ALL_CAPS_WITH_UNDERSCORES</code>		
Field name: capsAfterFirstWord. name must be meaningful outside of context		
<b>IDIOMATIC METHODS:</b> Are names compliant with the following rules?	yes	no
Method name: capsAfterFirstWord		
Local variables: capsAfterFirstWord.		
Name may be short (e.g., <code>i</code> for an integer) if scope of declaration and use is less than 30 lines.		
Factory method for X: <code>newX</code>		
Converter to X: <code>toX</code>		
Getter for attribute x: <code>getX()</code>		
Setter for attribute x: <code>void setX</code>		



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# Example

## Java Checklist: Level 2 inspection (comprehensive review in context)

FEATURES (where to look and how to check):

Item (what to check)

DATA STRUCTURE CLASSES: Are the following requirements satisfied?	yes	no	comments
The class keeps a design secret			
The substitution principle is respected: Instance of class can be used in any context allowing instance of superclass or interface			
Methods are correctly classified as constructors, modifiers, and observers			
There is an abstract model for understanding behavior			
The structural invariants are documented			
FUNCTIONAL (STATELESS) CLASSES: Are the following requirements satisfied?	yes	no	comments
The substitution principle is respected: Instance of class can be used in any context allowing instance of superclass or interface			
METHODS: Are the following requirements satisfied?	yes	no	comments
The method semantics are consistent with similarly named methods. For example, a "put" method should be semantically consistent with "put" methods in standard data structure libraries			
Usage examples are provided for nontrivial methods			
FIELDS: Are the following requirements satisfied?	yes	no	comments
The field is necessary (cannot be a method-local variable)			
Visibility is protected or private, or there is an adequate and documented rationale for public access			
Comment describes the purpose and interpretation of the field			
Any constraints or invariants are documented in either field or class comment header			
DESIGN DECISIONS: Are the following requirements satisfied?	yes	no	comments
Each design decision is hidden in one class or a minimum number of closely related and co-located classes			
Classes encapsulating a design decision do not unnecessarily depend on other design decisions			
Adequate usage examples are provided, particularly of idiomatic sequences of method calls			
Design patterns are used and referenced where appropriate			
If a pattern is referenced: The code corresponds to the documented pattern			



# Documenting Test Cases (see IEEE #829-1998)

- Of course, the overall testing strategy must be documented
  - exactly as it is the case for software
- For software development, you have many frameworks available
  - UML diagrams or similar
- There does not exist a testing equivalent
- Different companies represent their testing strategy using proprietary methods
- We can however say which elements are typically present in a testing strategy or *test plan*



# Test Plan Items

- System Under Verification
  - may be composed by many subsystems
  - includes at least one between code and documentation
- Testing objectives and rationale
  - which parts should be checked first and/or more thoroughly
- Scope and limitation of the test plan
  - you cannot test everything



# Test Plan Items

- Sources of expertise for test planning and execution
  - both economic and technical
- Sources of test data
  - may be automatically (randomly or deterministically) generated, taken from some Web site and/or book, etc
- Test environments and their management
  - scaffolding description



# Test Plan Items

- Testing strategy
  - given a development stage...
    - early, first prototype, first release, etc
  - ... decide which testing methodology use
    - static testing, white-box testing, black-box testing, performance testing
  - could also take into account not only the application, but its environment, e.g., connectivity
- Overall testing schedule



# Test Plan Items

- For each development phase defined in the testing strategy, document the following:
  - the development phase
    - early, first prototype, first release, etc
  - requirements for starting testing
    - e.g.: software have successfully compiled
  - requirements for ending testing
    - e.g.: 10% coverage acquired, all test passed
  - test case specifications
    - together with writing schedule, executing schedule and analysis/reporting schedule
    - will be back later on this
    - core of the testing phase



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# Test Plan Items

- Many items will need refinement during the process itself, due to:
  - errors being discovered at high stage: correcting them cause changes in lower stages, also testing is affected
  - same for modifications not strictly coming from errors
  - new releases of software
  - for early drafts of the test plan, there may not be enough information, thus many draft releases are needed



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